



3DV 2018 Tutorial

# Material appearance measurement

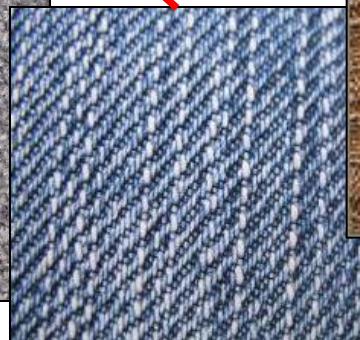
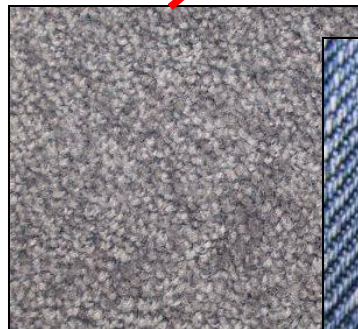
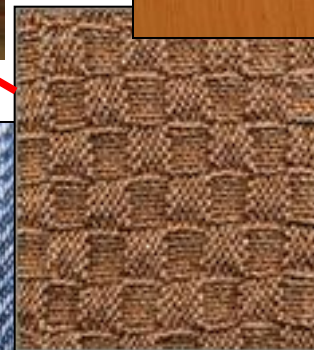
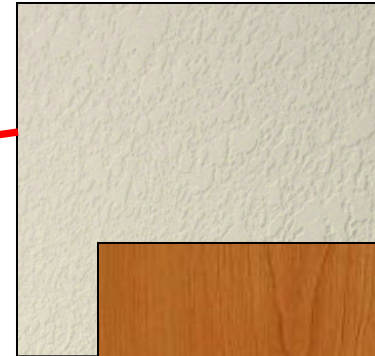
Jiri Filip

Institute of Information Theory and Automation  
of the AS CR

September 8, 2018

# Motivation for appearance measurement

- Materials in real world



# Our mission

- Digital reproduction of material appearance

real world



Measurement



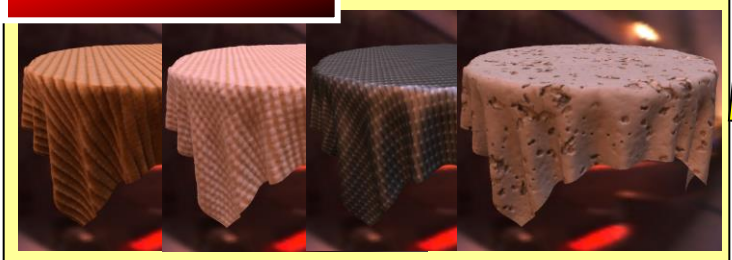
digital world



Accurate  
Appearance  
Measurement



Visualization



Visual Scene Analysis



$$Y_r = \gamma X_r + e_r$$

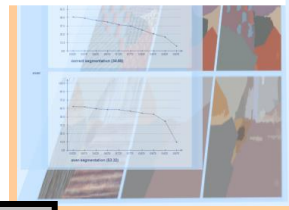
Interior Design



Culture Heritage  
Digitization



Scene Segmentation



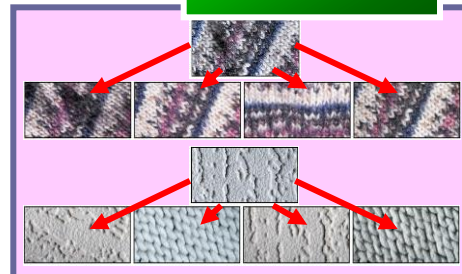
Visual  
Psychophysics



Visual Safety  
Simulation



Image  
retrieval



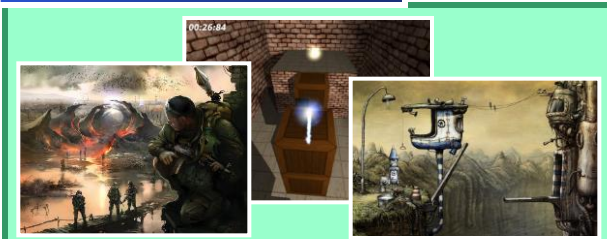
Medical  
Images  
Analysis



Movie Industry

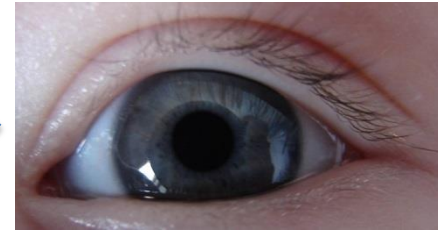


Game Industry

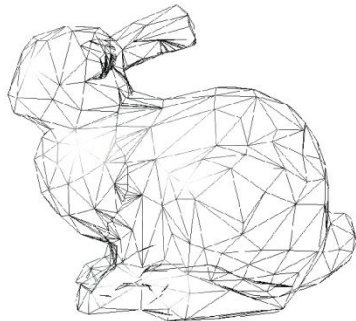


# Digital Material Appearance

Virtual Environment



Shapes  
3D Geometry



Illumination  
conditions



Material  
Appearance

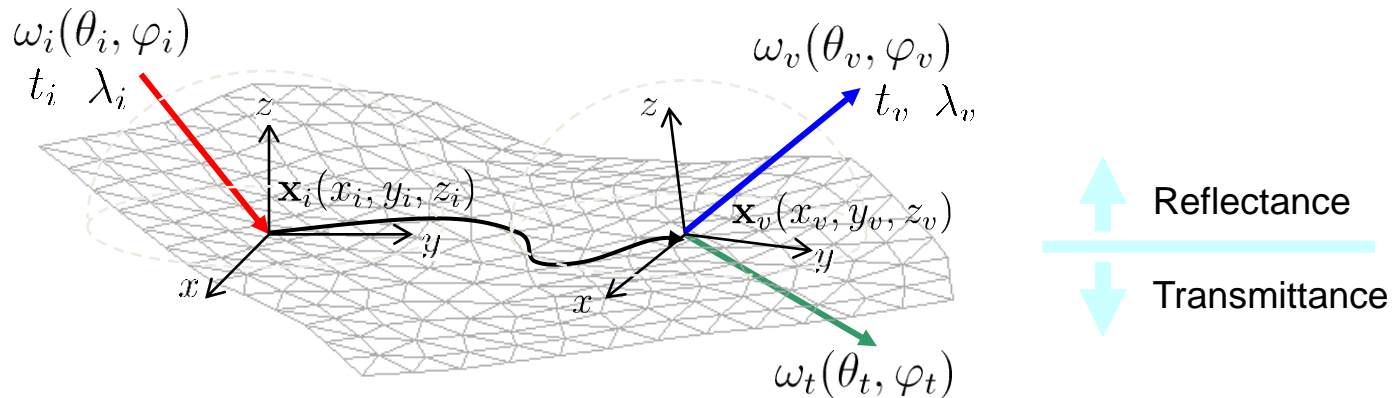


# Outline

1. Taxonomy of material appearance representations
2. Measurement approaches
  - BRDF
  - SVBRDF
  - BTF
3. Angular parameterizations
4. Anisotropic vs. isotropic BRDF
5. Uniform vs. adaptive measurement strategies
6. Publicly available datasets

# Light-Material Interaction

## General Reflectance Function

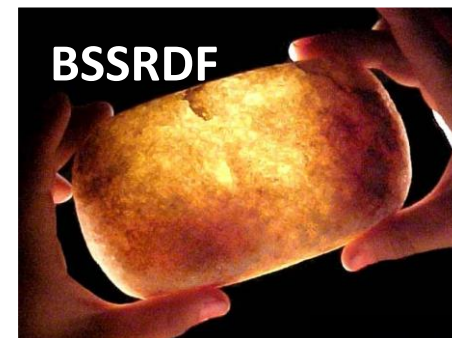
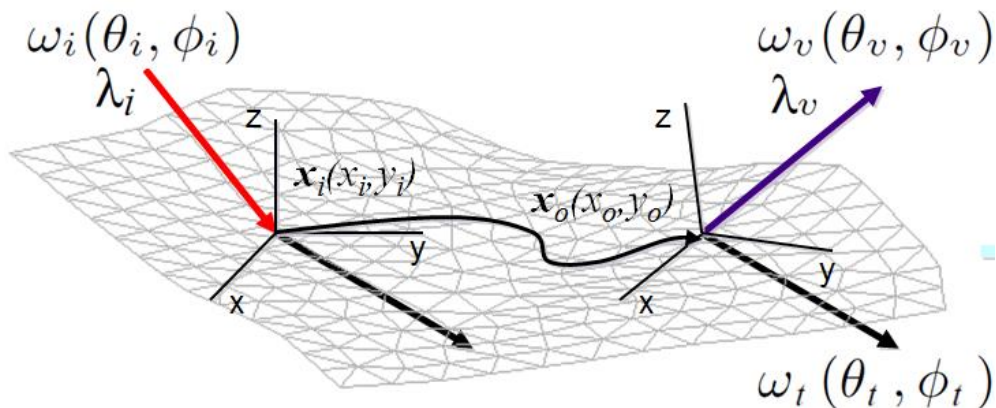


$$Y_r = GRF(\lambda_i, x_i, y_i, z_i, t_i, \theta_i, \varphi_i, \lambda_v, x_v, y_v, z_v, t_v, \theta_v, \varphi_v, \theta_t, \varphi_t)$$

16 dimensions

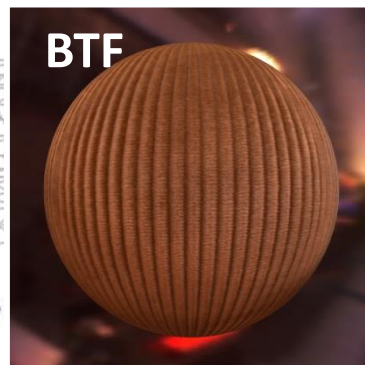
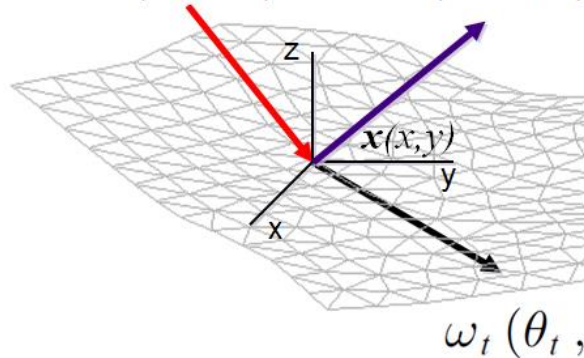
# Light-Material Interaction

## General model of light-material interaction



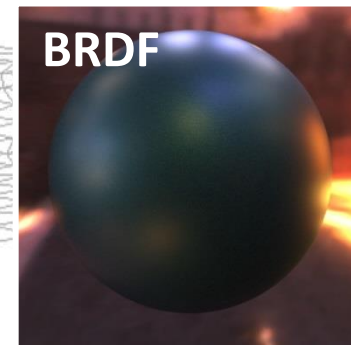
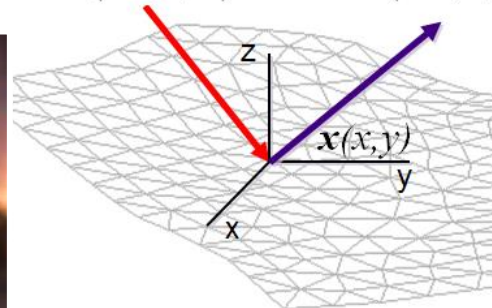
## Local scattering effects only

$\omega_i(\theta_i, \phi_i)$        $\omega_v(\theta_v, \phi_v)$



## Opaque flat materials

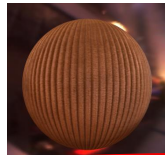
$\omega_i(\theta_i, \phi_i)$        $\omega_v(\theta_v, \phi_v)$



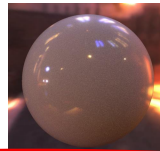


# Taxonomy of Material Appearance Representations

Textured materials



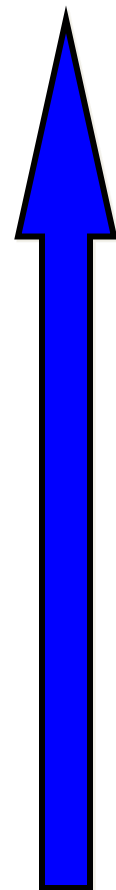
Homogeneous materials



Complexity of measurement and modelling



High



Low



Reflectance Fields / BSSRDF

$$(\lambda, x_i, y_i, \theta_i, \varphi_i, x_v, y_v, \theta_v, \varphi_v)$$

Bidirectional surface scattering reflectance distribution function

Spatially varying BRDF

SVBRDF

Bidirectional texture function

BTF

Bidirectional scattering distribution function

BSDF

$$(\lambda, x, y, \theta_i, \varphi_i, \theta_v, \varphi_v)$$

$$(\lambda, \theta_i, \varphi_i, \theta_v, \varphi_v, \theta_t)$$

Surface light field

SLF

Surface reflectance field

SRF

Bidirectional reflectance / transmittance distribution functions

BRDF

BTDF

$$(\lambda, x, y, \theta_v, \varphi_v)$$

$$(\lambda, x, y, \theta_i, \varphi_i)$$

$$(\lambda, \theta_i, \varphi_i, \theta_v, \varphi_v)$$

$$(\lambda, \theta_i, \varphi_i, \theta_t, \varphi_t)$$

Dynamic Texture

$$(\lambda, x, y, t)$$

Texture, bump-map, albedo map, etc.

Isotropic BRDF

$$(\lambda, \theta_i, \theta_v, |\varphi_i - \varphi_v|)$$

Multispectral Texture

$$(\lambda, x, y)$$

9D

7D

5D

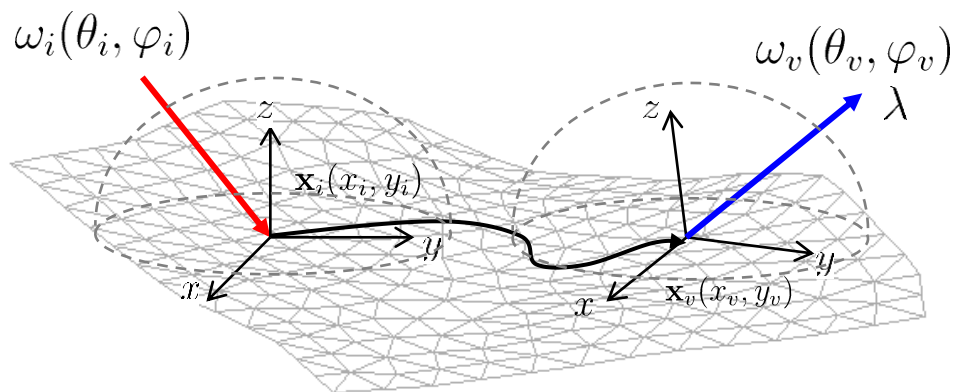
4D

3D

# Textured Materials Representations

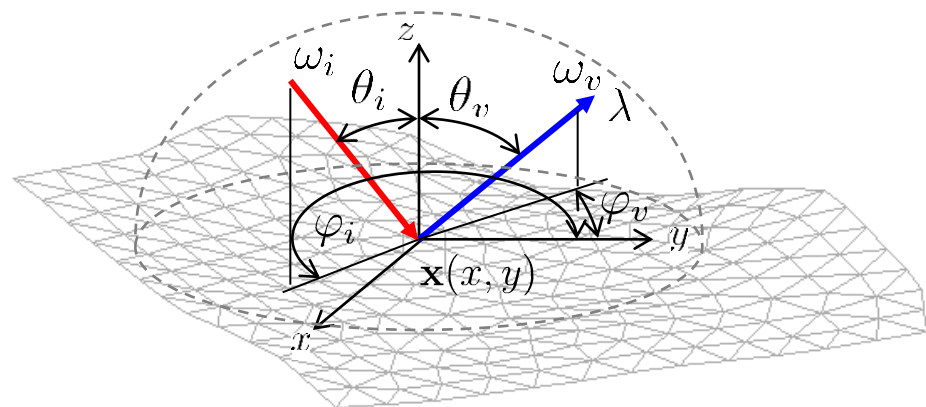
**BSSRDF**

9D



**BTF / SVBRDF**

7D



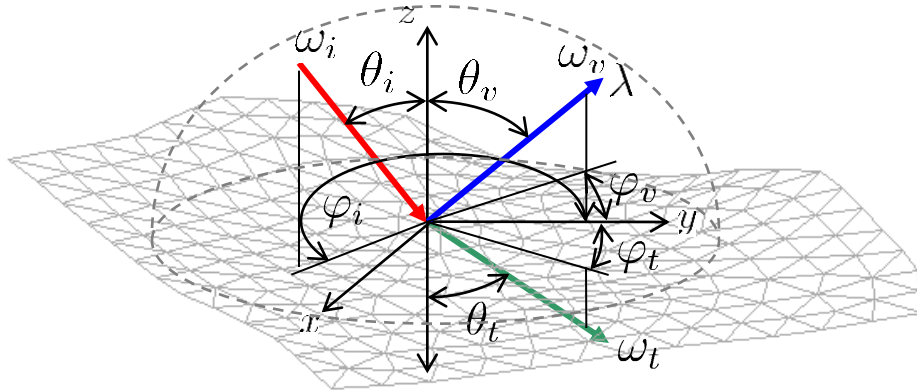
$$Y_r = BSSRDF(\lambda, x_i, y_i, \theta_i, \varphi_i, x_v, y_v, \theta_v, \varphi_v)$$

$$Y_r = BTF(\lambda, x_i, y_i, \theta_i, \varphi_i, \theta_v, \varphi_v)$$

# Homogeneous Materials Representations

**BSDF**

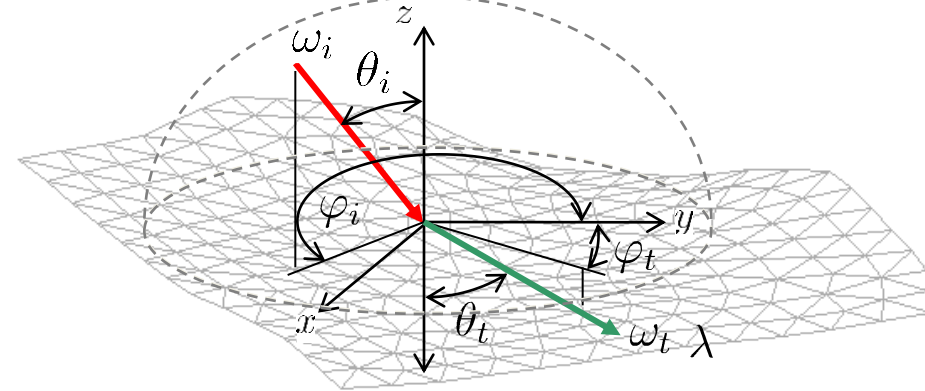
**7D**



$$Y_r = BSDF(\lambda, \theta_i, \phi_i, \theta_v, \phi_v, \theta_t, \phi_t)$$

**BTDF anisotropic**

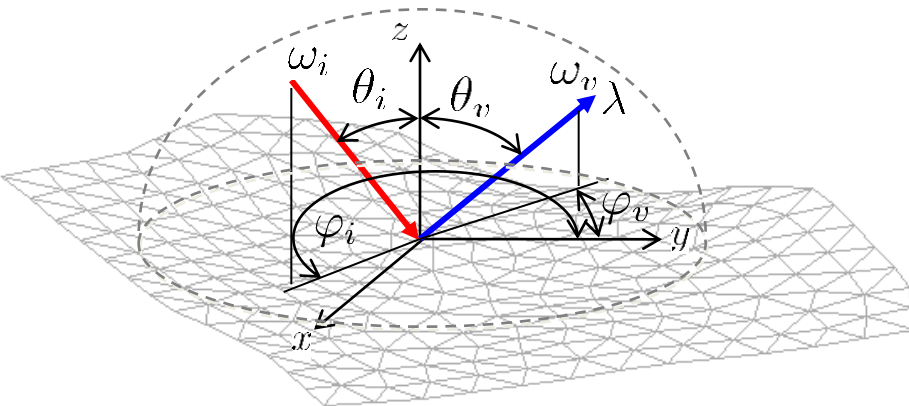
**5D**



$$Y_r = BTDF(\lambda, \theta_i, \phi_i, \theta_t, \phi_t)$$

**BRDF anisotropic**

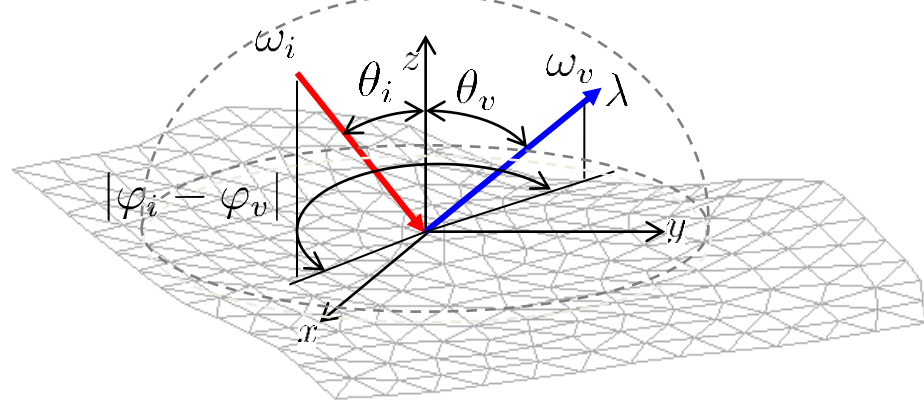
**5D**



$$Y_r = BRDF(\lambda, \theta_i, \phi_i, \theta_v, \phi_v)$$

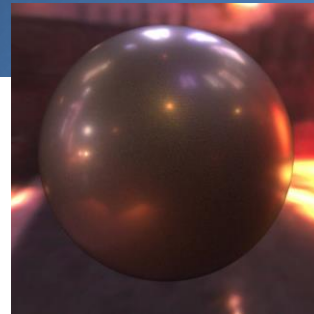
**BRDF isotropic**

**4D**



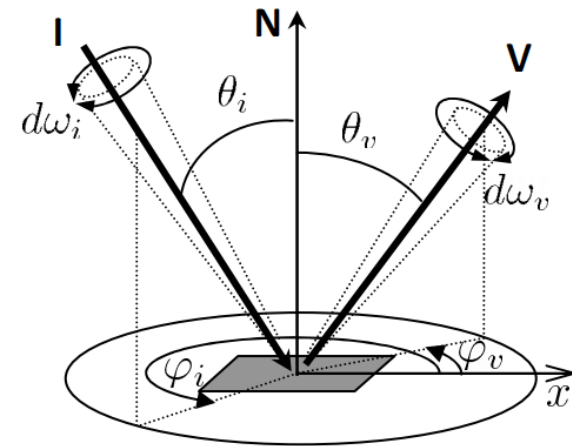
$$Y_r = IBRDF(\lambda, \theta_i, \theta_v, |\phi_i - \phi_v|)$$

# Bidirectional Reflectance Distribution Function



- Distribution of radiance reflected (L)

$$BRDF(\lambda, \theta_i, \phi_i, \theta_v, \phi_v) = \frac{dL_r(\lambda, \theta_v, \phi_v)}{\underbrace{L_i(\lambda, \theta_i, \phi_i) \cos \theta_i d\omega_i}_{\text{irradiance } E_i}}$$



- **Properties**

- Illum./view directions reciprocity

- swapping source and sensor does not effect BRDF value

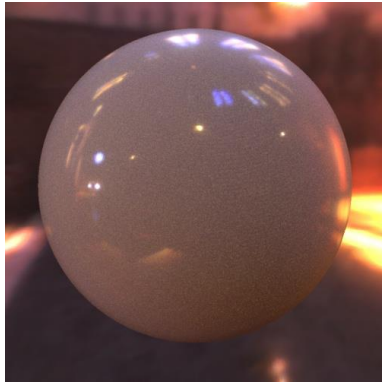
- Energy conservation

- portion of energy reflected to all directions has to be between 0 and 1

$$\int_{\Omega} BRDF(\lambda, \theta_i, \phi_i, \theta_v, \phi_v) \cos \theta_v d\omega_v \leq 1$$

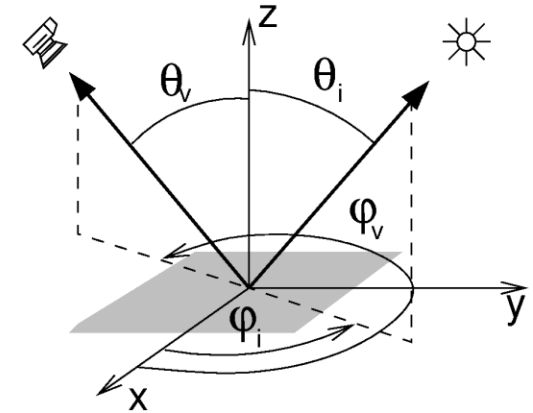
- Non-negativity

# BRDF Measurement Setups Taxonomy



$$BRDF(\lambda, \theta_i, \varphi_i, \theta_v, \varphi_v)$$

**5 dimensional data**  $\Leftrightarrow$  4 dimensions depend on camera, light & sample positioning



Measurement setup with **4 mechanical degrees of freedom**:

Gonio-reflectometers

sample/light/camera **1/2/1**

Mirror-based setups

sample/light **2/2** + many views at once

Image-based setups

light/camera **1/1** + defined shape

Portable setups

compromise accuracy measurements

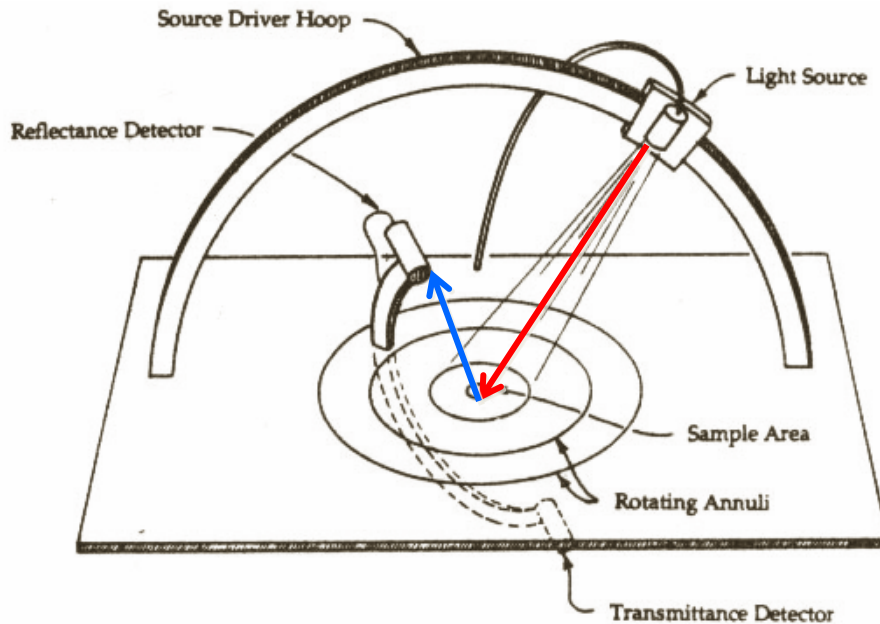
Isotropic BRDF (4 dimensional):  $BRDF(\lambda, \theta_i, \theta_v, \varphi_i - \varphi_v)$

# BRDF Sample Acquisition

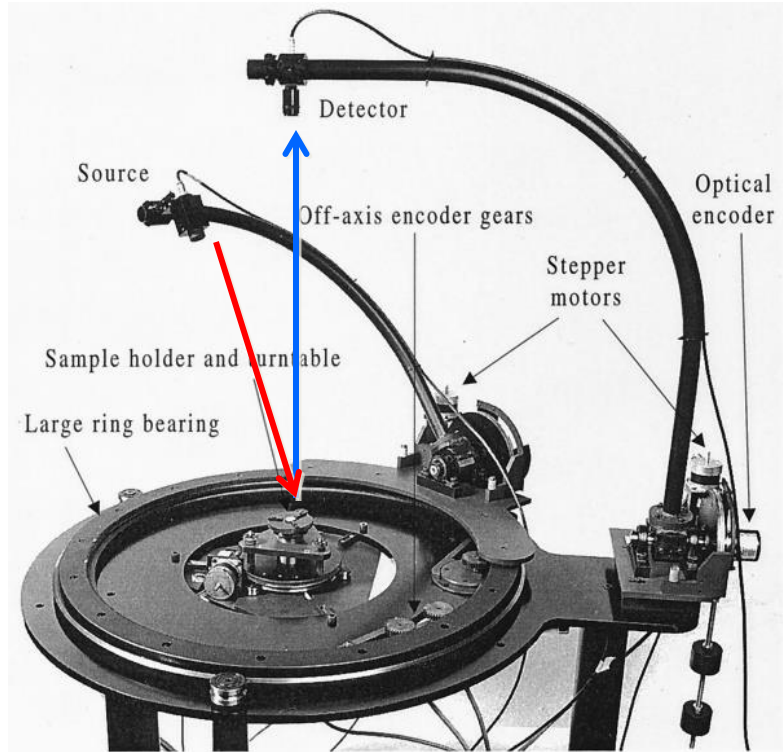
## Gonio-reflectometers

Sequential sampling of 4D space  $\Rightarrow$   
moving sample, light & camera

[Murray & Smith JIES 90]



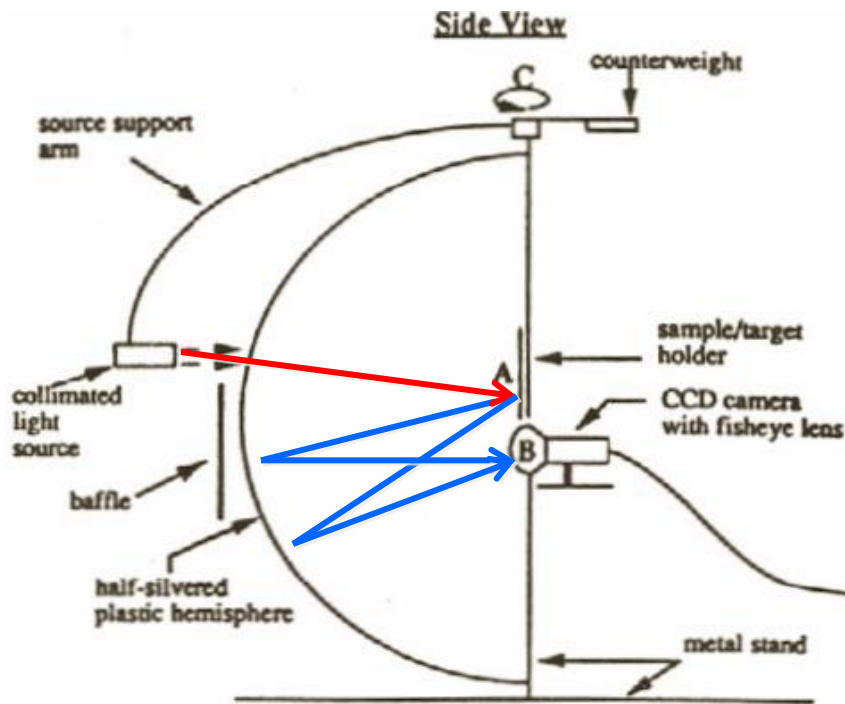
[White et al. JAO 98]



# BRDF Sample Acquisition

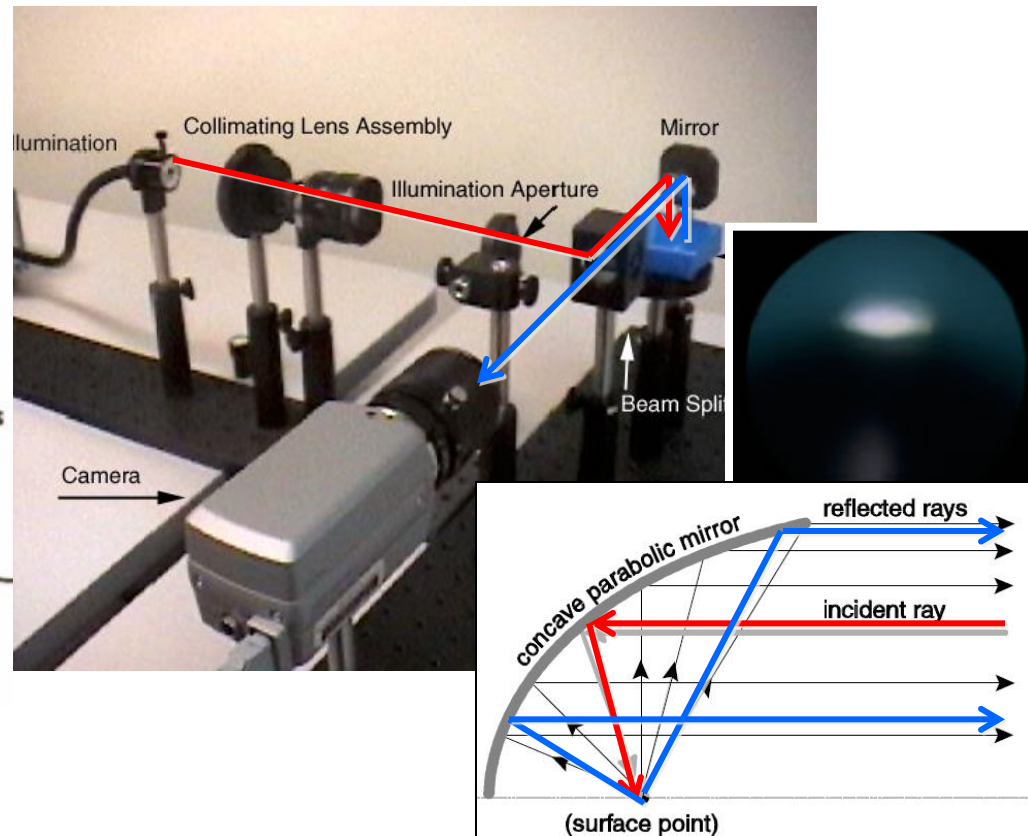
## Mirror-based setups

[Ward CG 92]



Mechanical DOF reduced by multiple-views in mirror image (directional illumination)

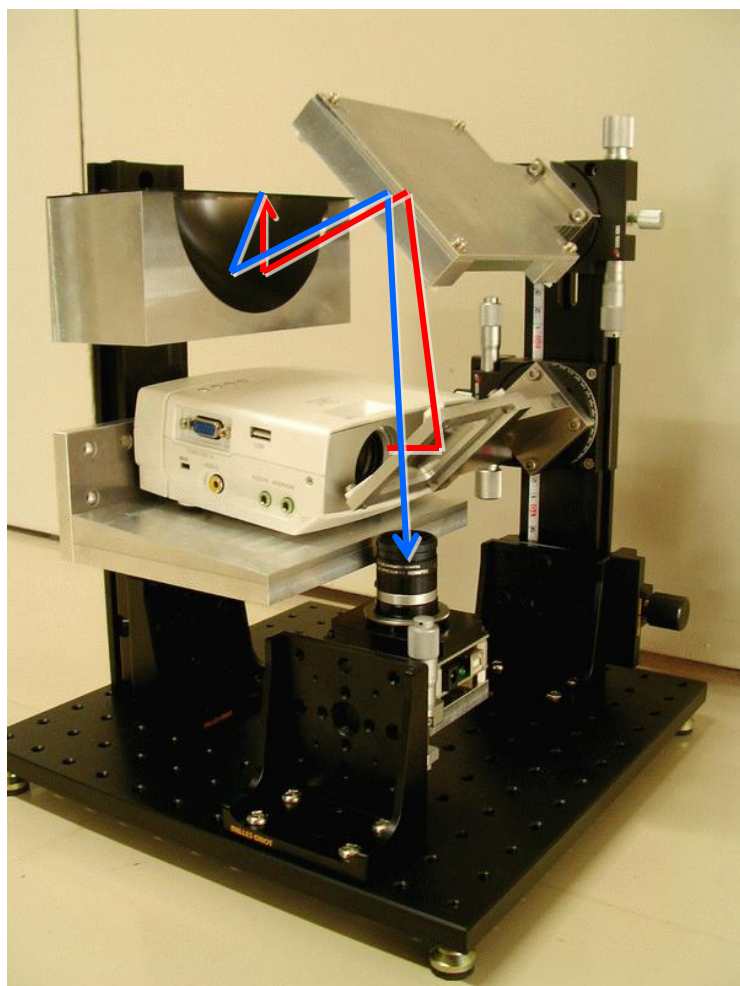
[Dana et al. ICCV 01]



# BRDF Sample Acquisition

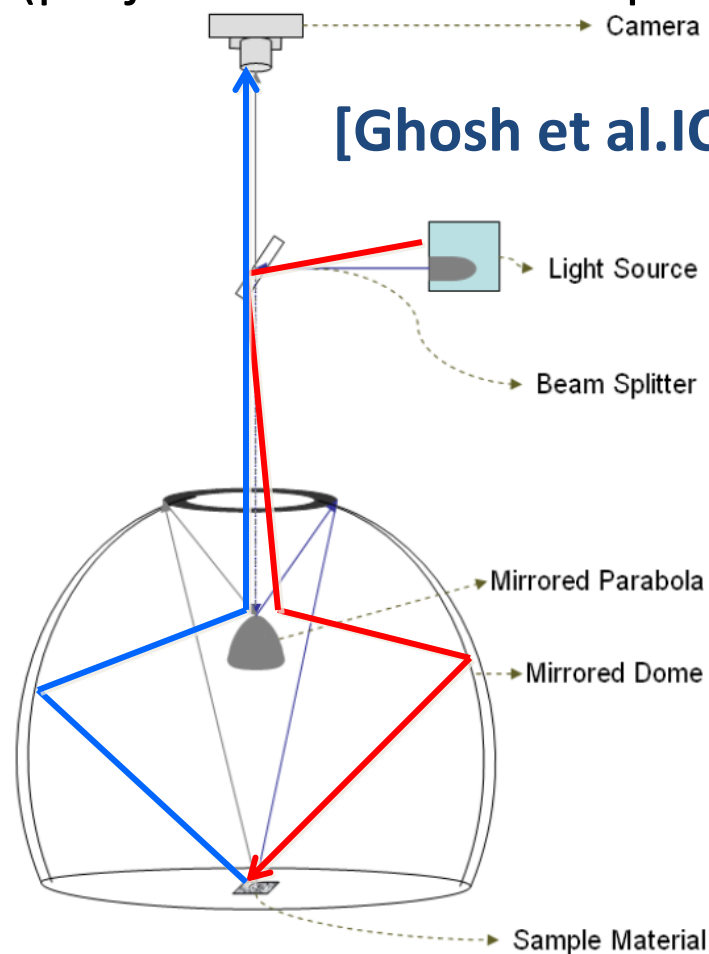
## Mirror-based setups

[Mukaigawa et al. ACCV 07]



Mechanical DOF reduced by multiple-views in mirror image (projected illumination pattern)

[Ghosh et al. ICCV 07]

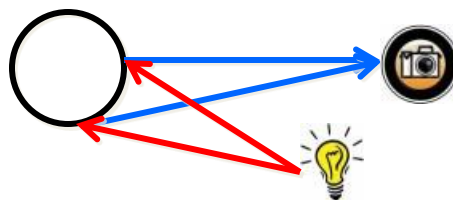




# BRDF Sample Acquisition

## Image-based setups

Varying incoming  
/outgoing directions  
over **cylinder** image



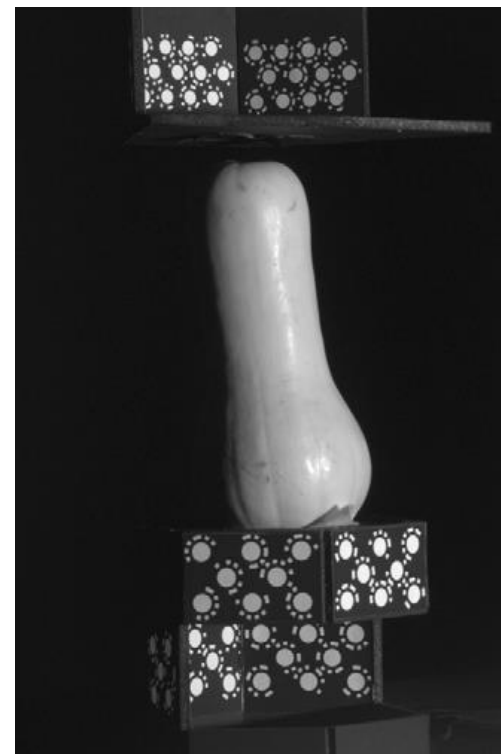
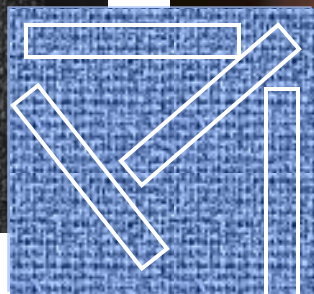
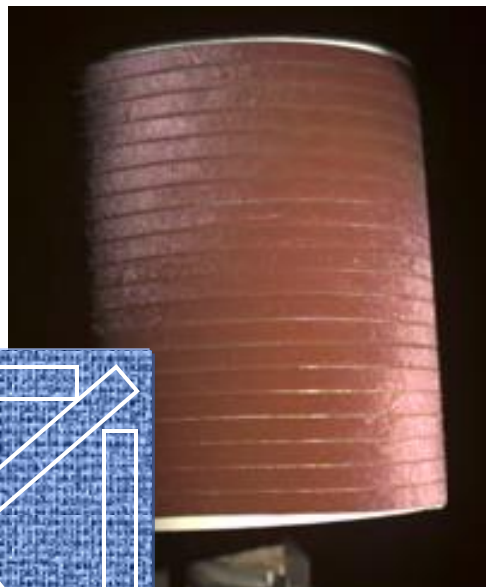
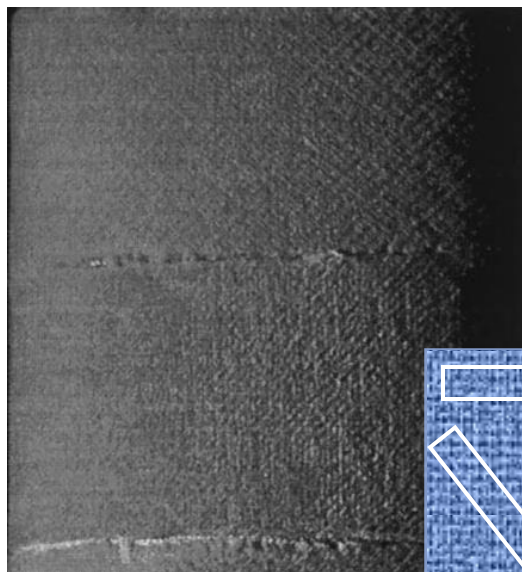
Mechanical DOF reduced by defined  
sample shape (orientation)

[Marschner et al. JAO 00]

object of estimated geometry

[Lu et al. JAO 98]

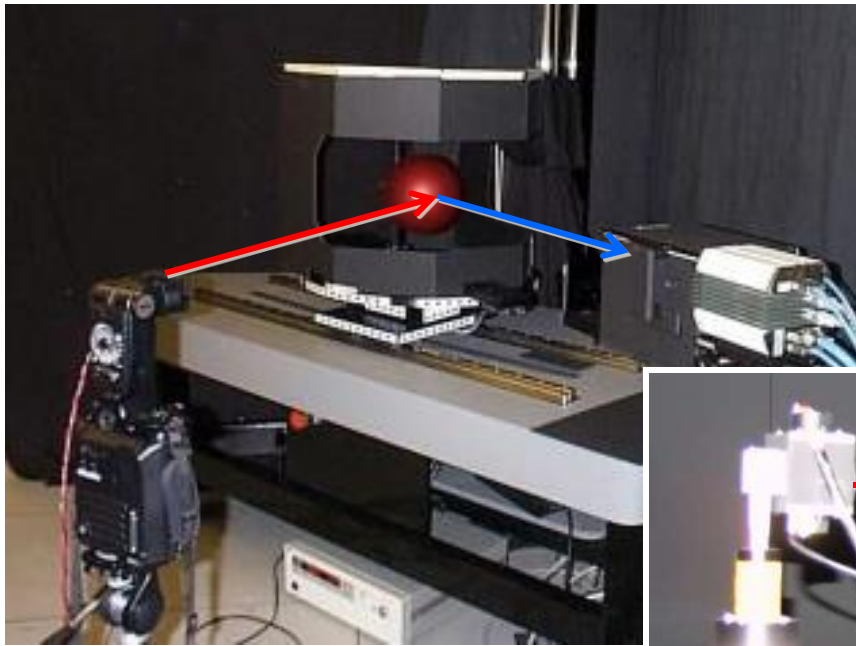
[Ngan et al. EGSR 05]



# BRDF Sample Acquisition

Image-based setups

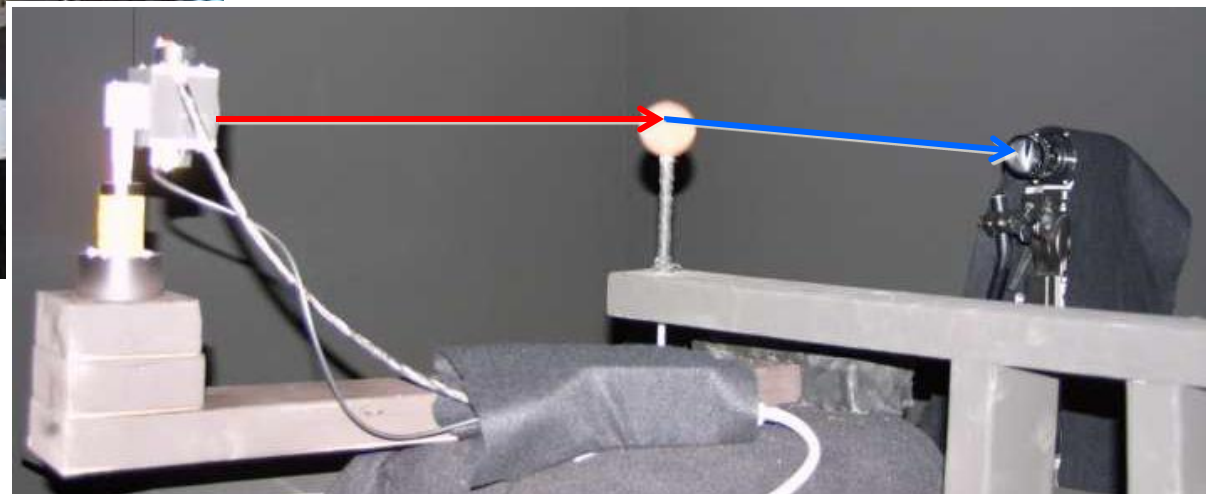
[Marschner PhD 98]



Mechanical DOF reduced by defined sample shape (orientation)

**Spherical** homogeneous samples

[Matusik et al. EWR 03]



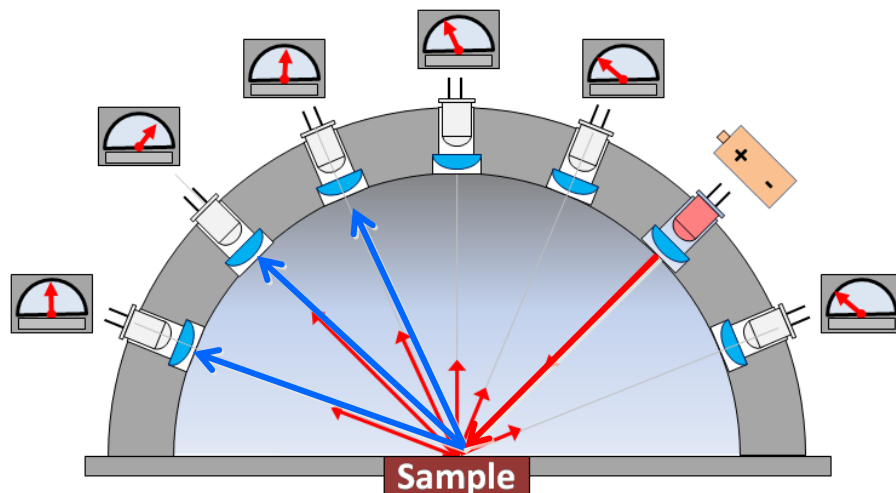
# BRDF Sample Acquisition

## Portable setups

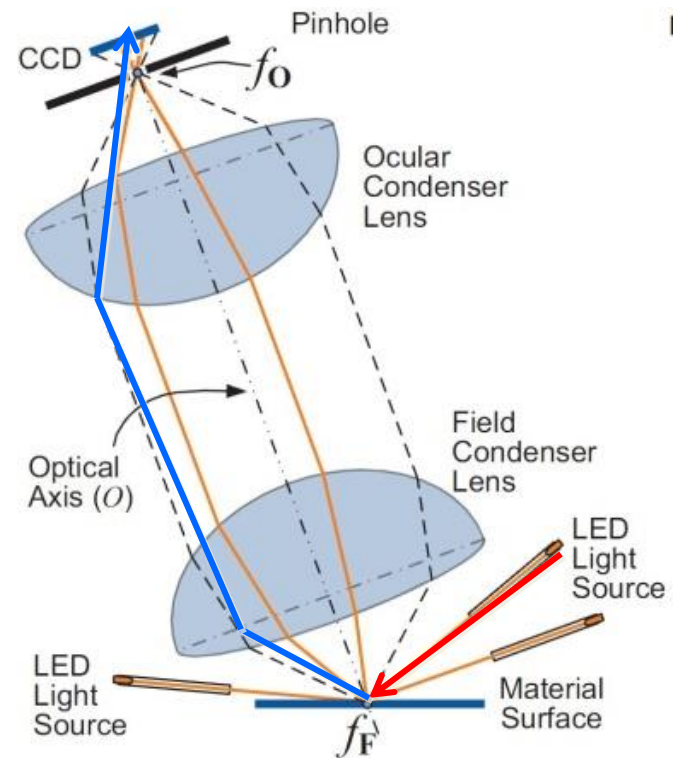
Fast measurement, compromise accuracy, limited:

- number of illumination/sensing elements
- viewing/illumination angles range

### [Ben-azra et al. CVPR 08]

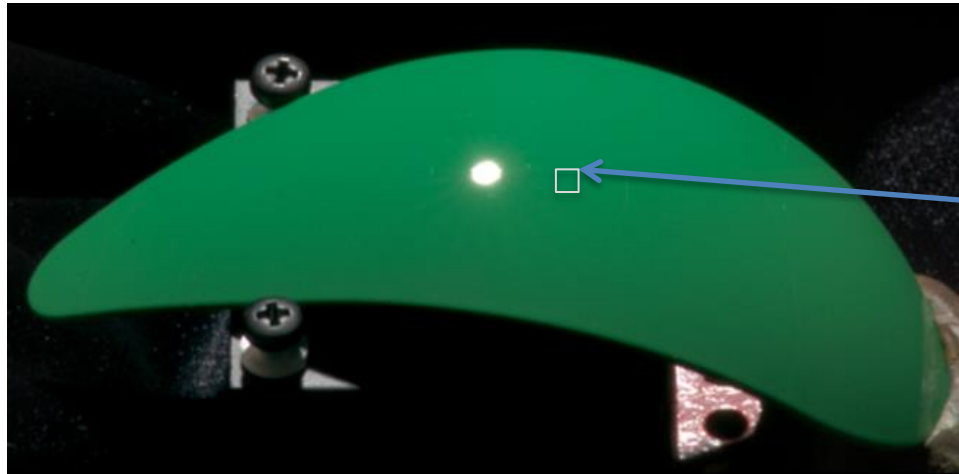


### [Lan et al. CGF 10]



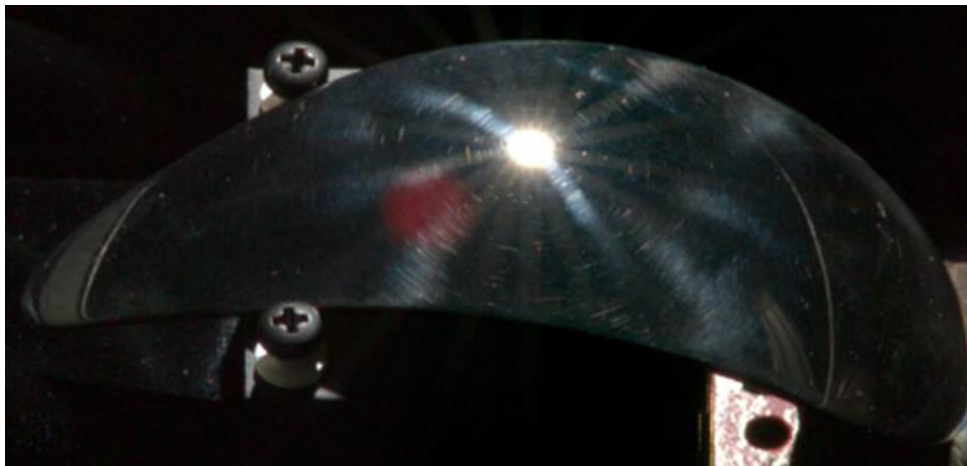
# Measurement of Specular BRDFs

Green paint with thick acrylic coating



Measured  
area 3x3 mm

Silver 925 (silver 92.5%, copper 7.5%)

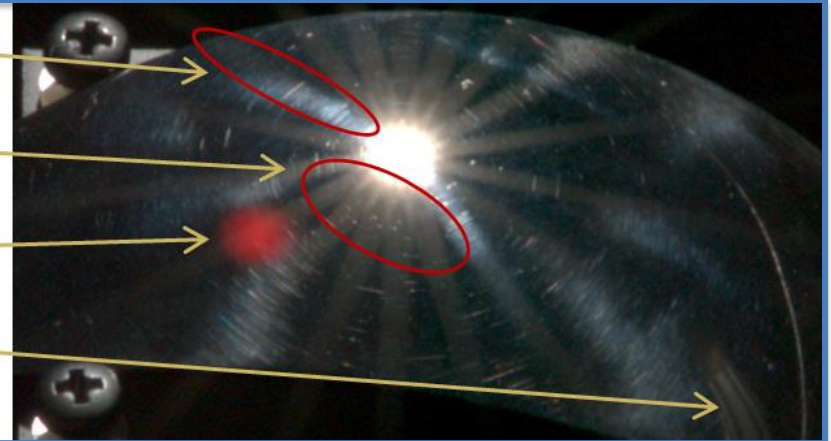


Shape courtesy of Lechler S.p.a. Como, Italy



# Measurement-related issues

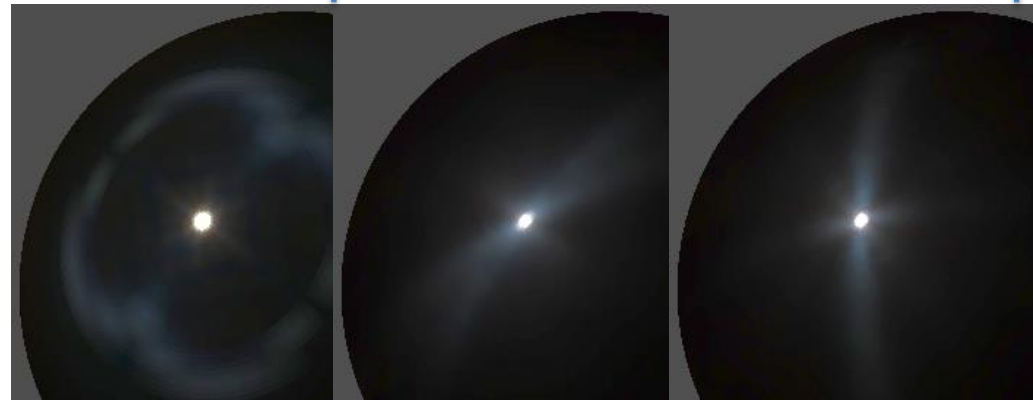
- anisotropy due to polishing
- light refraction on aperture
- lens flare artifact
- reflections of environment



## Anisotropic artifacts

- due to insufficient polishing
- highlight perpendicular to scratches
- can be avoided by selecting appropriate

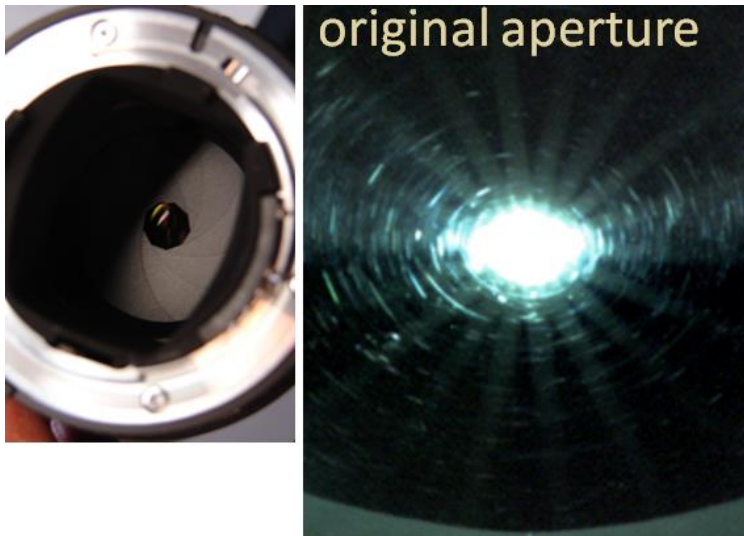
BRDFs from MERL database cannot be safely used as a reference



# Measurement-related issues

## Diffraction on aperture

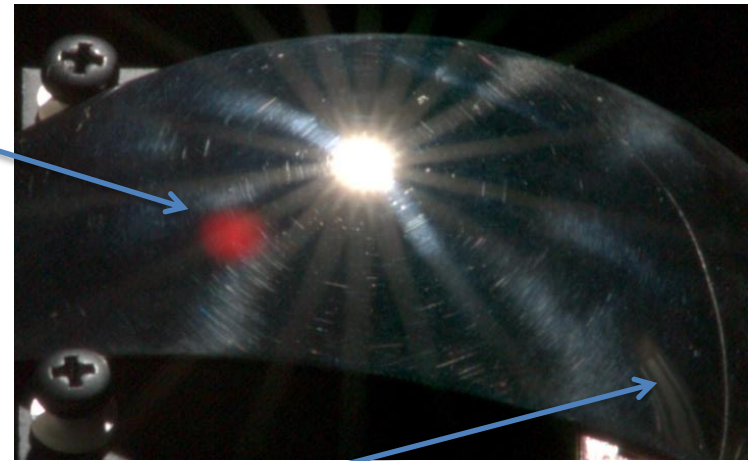
- wave effect of light  $\Rightarrow$  light passing narrow slit
- bright streak perpendicular to aperture blades
- streaks in both directions  $\Leftrightarrow$  odd number of blades  $\Rightarrow$  twice so many streaks
- pronounced for narrow aperture and bright point-light
- solved by circular aperture



# Measurement-related issues

## Lens flare

- usually red spot due to inter-reflection in lens body
- the more elements the more pronounced
- Suppressed by a long lens hood

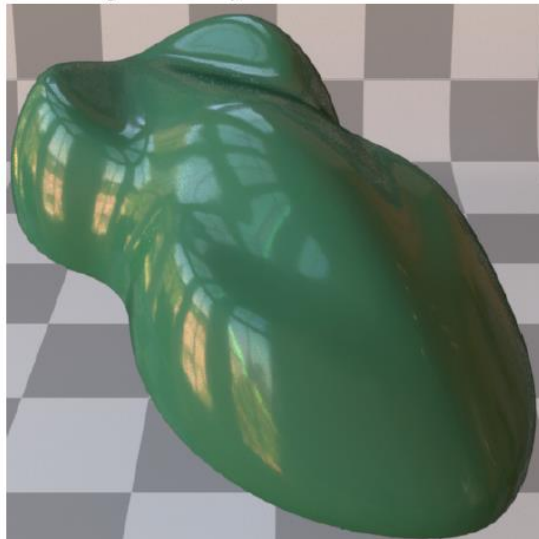


## Reflection from environment

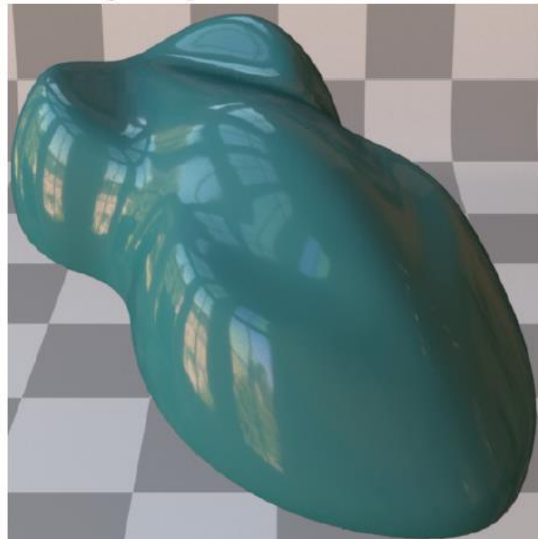
- mirror-like finishes reflect environment – diffuse black covering

# Results – specular BRDFs

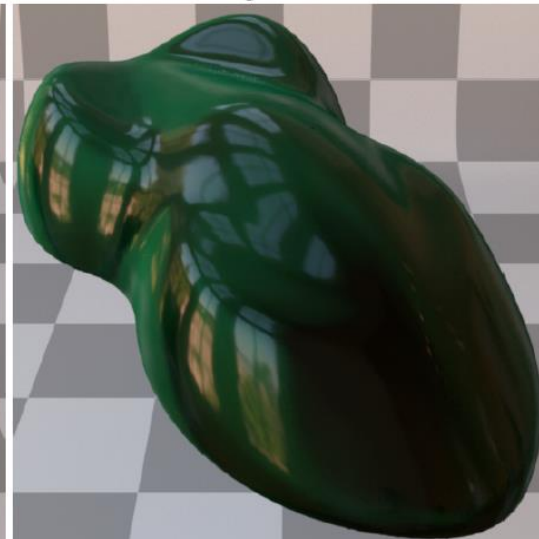
MERL *green-acrylic*



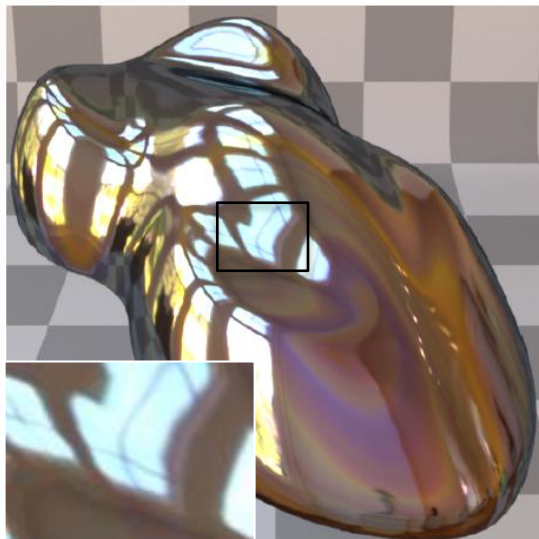
MERL *green-plastic*



our measurement paint



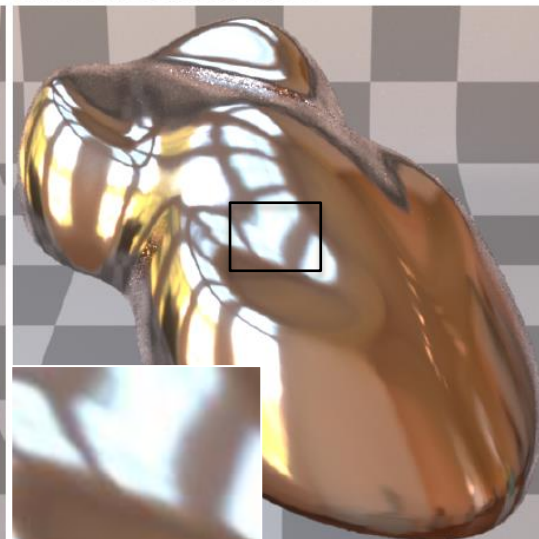
MERL *chrome*



MERL *steel*



our measurement silver





# Spatially-Varying BRDF Measurement

[McAllister 02]



$$SVBRDF(\lambda, x, y, \theta_i, \varphi_i, \theta_v, \varphi_v)$$

- **7 dimensional data**  $\Leftrightarrow$  4 dimensions depend on camera, light & sample positioning
- Restricted to opaque, flat surfaces where BRDF reciprocity holds

Measurement setup with **4 mechanical degrees of freedom**:

Gonio-reflectometers

sample/light/camera **1/2/1**

Image-based setups

sparse view/light sampling **2/2** +  
known geometry

Light-stages

many lights/cameras **2/2**

Portable setups

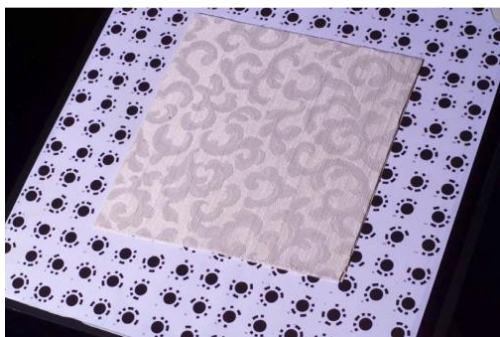
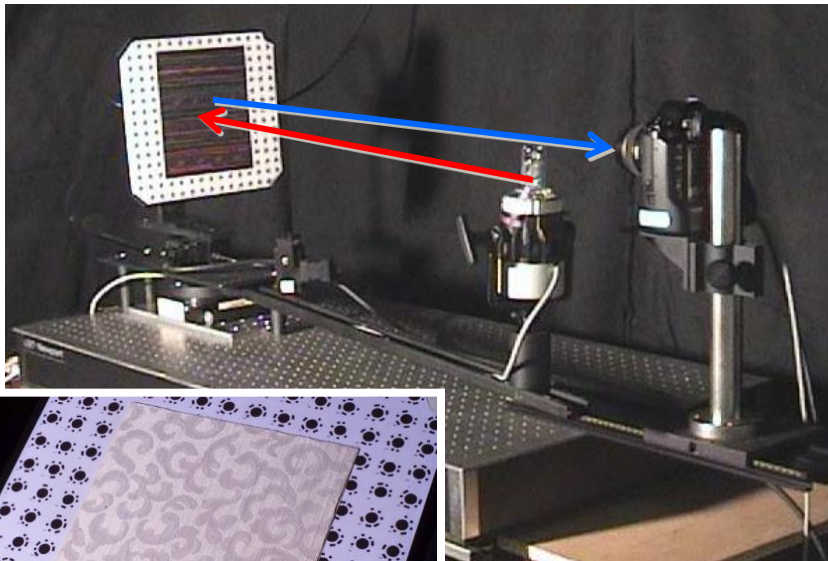
registration of BRDF measurement to  
sparse object images

# SV-BRDF Sample Acquisition

## Gonio-reflectometers

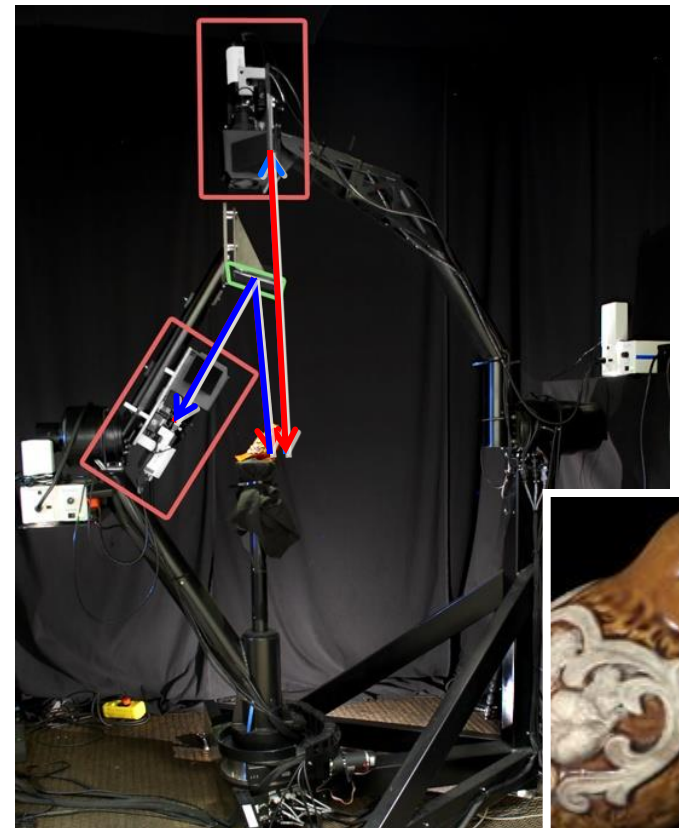
### [McAllister GH 02]

- moving light, tilting sample



### [Holroyd et al. TOG 10]

Simultaneous measurement  
of geometry and SVBRDF



# SV-BRDF Sample Acquisition

## Light stages

### Facial SVBRDF measurement

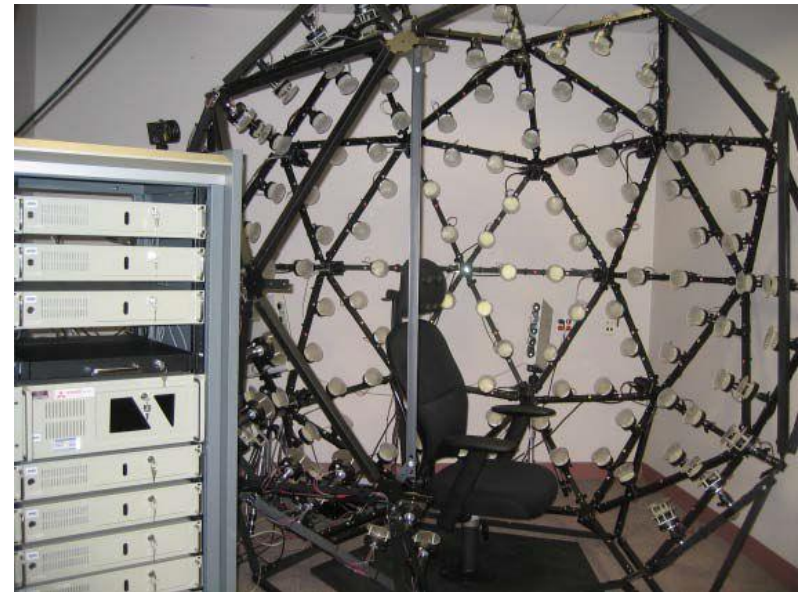
- 156 lights, high-speed camera

[Debevec et al. SIG 00]



- 150 lights, 16 cameras
- structured light for geometry capture

[Weyrich et al. SIG 06]

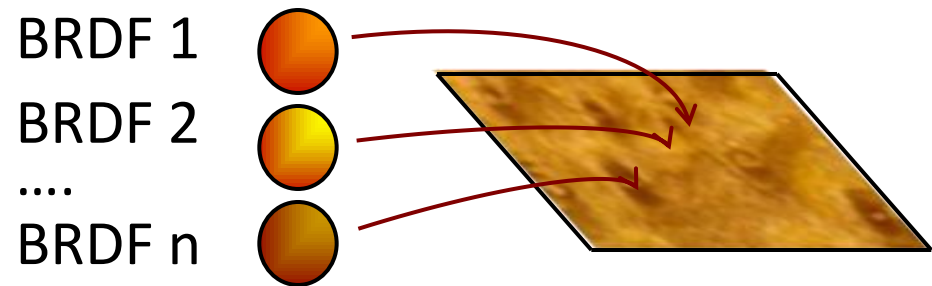


# SV-BRDF Sample Acquisition

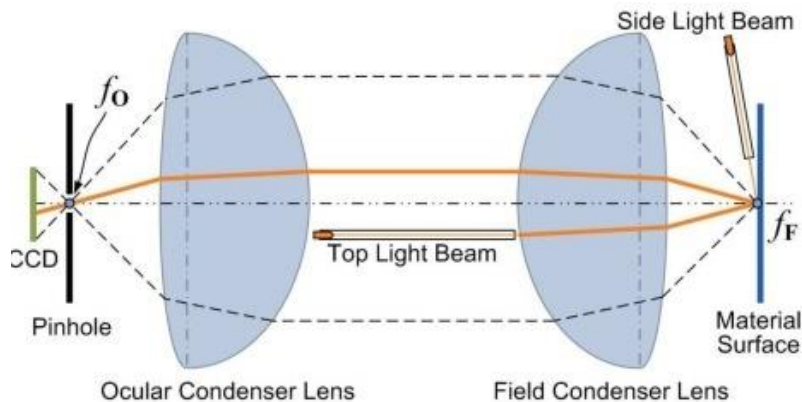
## Portable setups

Fast measurement, compromise accuracy:

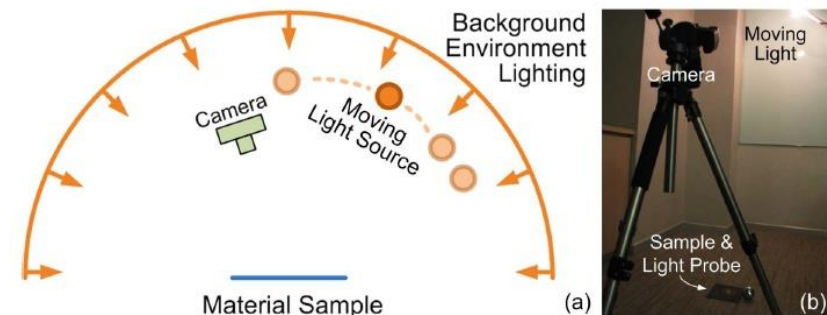
- Sparsely measured BRDF registered to measured object reflectance map (single view, many lights)
- Anisotropic BRDFs



[Dong et al. SIG 10]



BRDF measurement

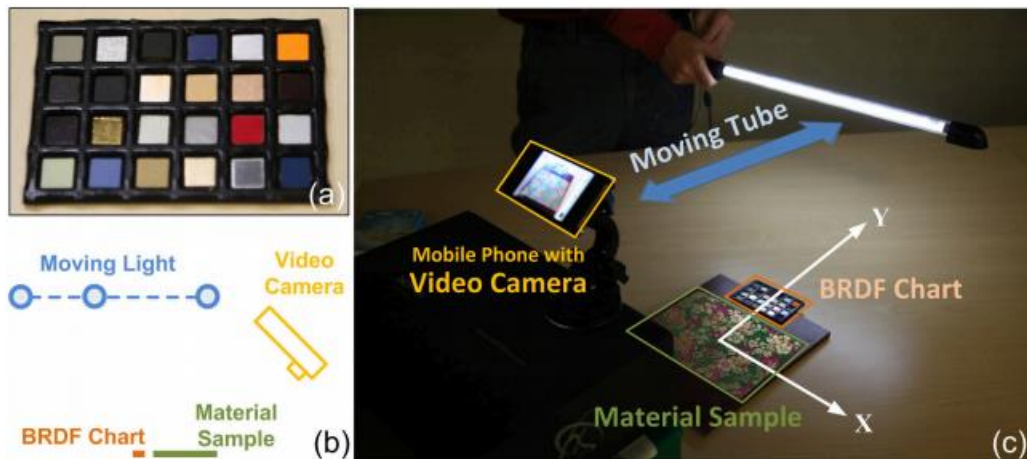


Reflectance-map measurement

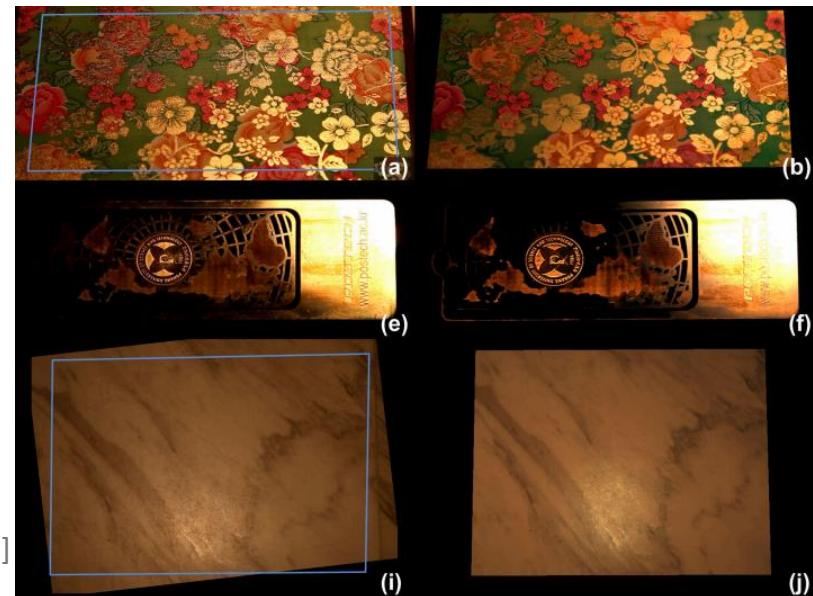
# SVBRDF Capture & Modeling

## Portable setups

- [Ren et al. TOG 11] - “pocket reflectometry”: SVBRDF from movie of static object lit by linear light source captured by a static mobile phone camera
  - Use set of BRDF reflectance targets (selection is important)
  - Measured reflectance fitted as a mixture of target’s BRDFs



[Ren et al. 11 ACM]



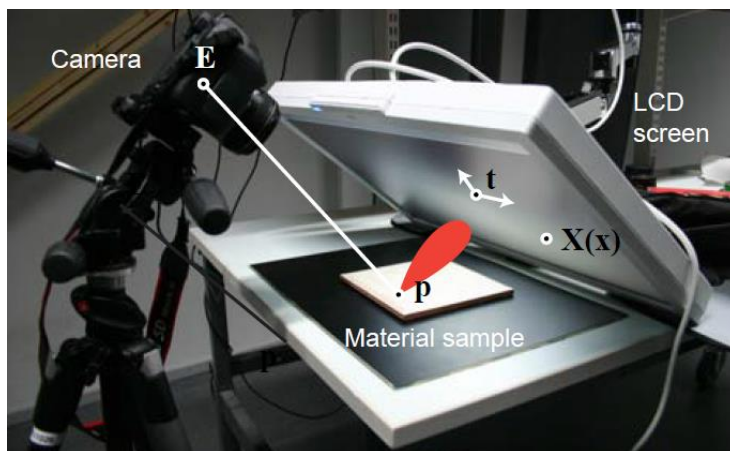
# SV-BRDF Sample Acquisition

Portable setups

[Aittala et al. SIGGRAPH 13]

## SVBRDF Capture In The Frequency Domain

- reflection of Fourier basis patterns emitted from the screen  $\Leftrightarrow$  fitting reflectance by Gaussian mixture models
- different sampling frequencies  $\Leftrightarrow$  131 images
- viewing rays reflecting into the screen as reflectance lobe
- each captured pixel  $\Leftrightarrow$  integral of the product of this projected lobe and the illumination pattern



# SV-BRDF Sample Acquisition

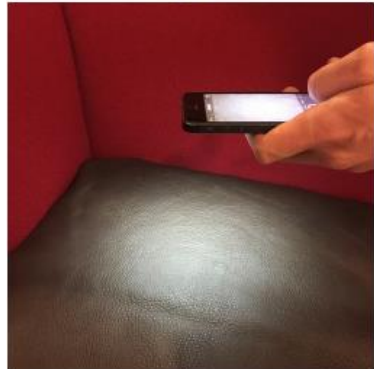
Portable setups

[Aittala et al. SIGGRAPH 15]

## Two-Shot SVBRDF Capture for Stationary Materials

- smartphone as capturing device
- acquisition limited to retroreflective BRDF slice  $\Rightarrow$  camera close to illumination
- fitting micro-facet BRDF model
- assumption of stationary texture in the material  $\Rightarrow$  repeatable structure

Capture



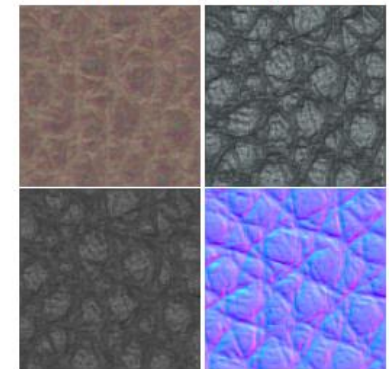
Flash image



No-flash image



SVBRDF Decomposition



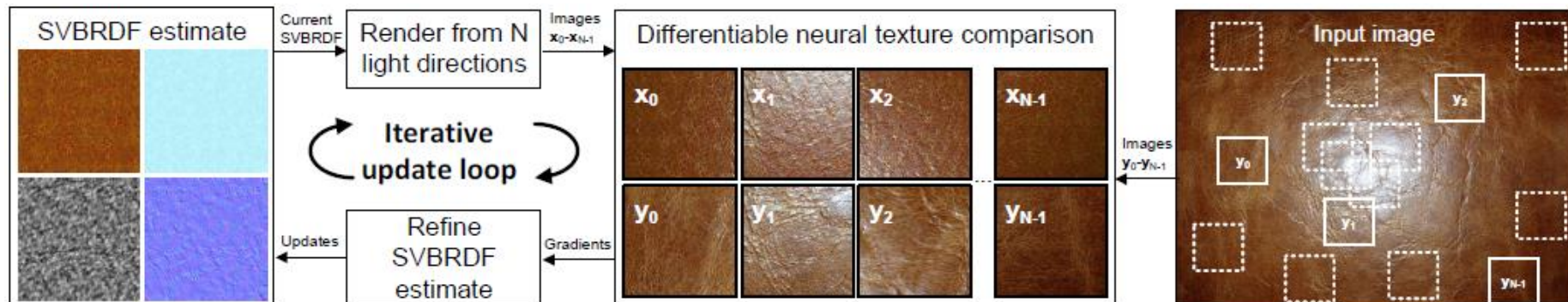
# SV-BRDF Sample Acquisition

Portable setups

[Aittala et al. SIGGRAPH 16]

## Reflectance Modeling by Neural Texture Synthesis

- spatially varying parametric reflectance models from a single image taken with flash illumination
- materials with stationary texture
- decomposition of image into local tiles
- deep convolutional neural network  $\Rightarrow$  fitting diffuse and specular coefficients maps



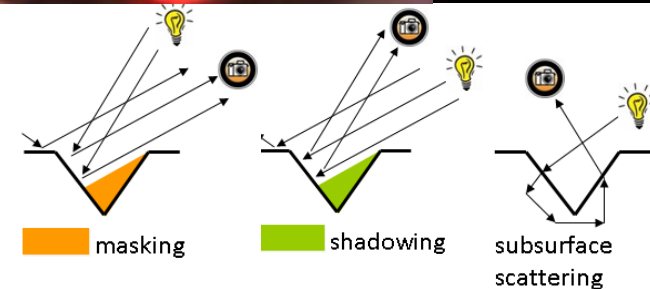
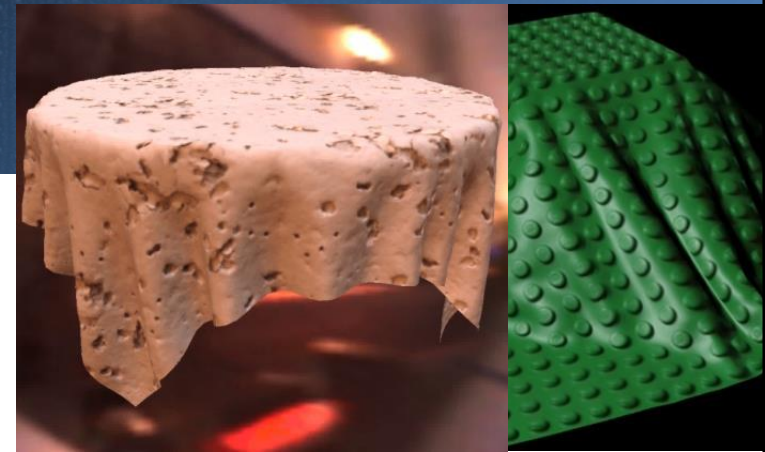


# Bidirectional Texture Function

- BTF – Bidirectional Texture Function
- Illumination/view directions dependent texture

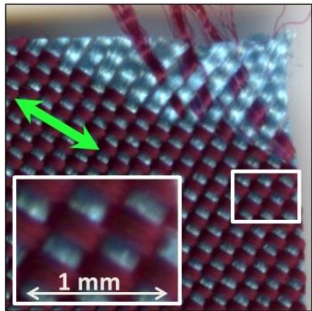
$$BTF(\lambda, x, y, \theta_i, \phi_i, \theta_v, \phi_v)$$

- Includes: inter-reflections, sub-surface scattering, local masking and shadowing
- One of the best practical representations of textured materials appearance
- Massive data  $\Leftrightarrow$  thousands of images per material (GBs)
- Compression and modelling is inevitable

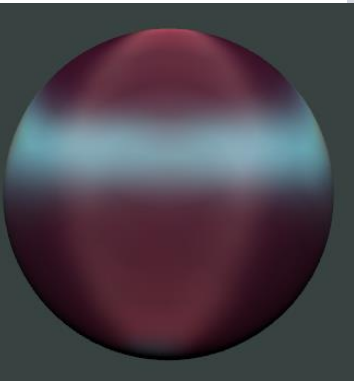
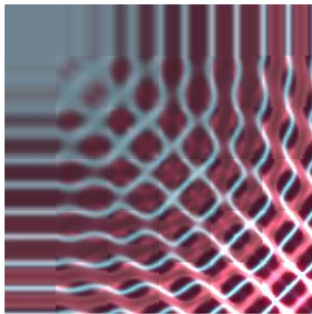


# BRDF vs. BTF

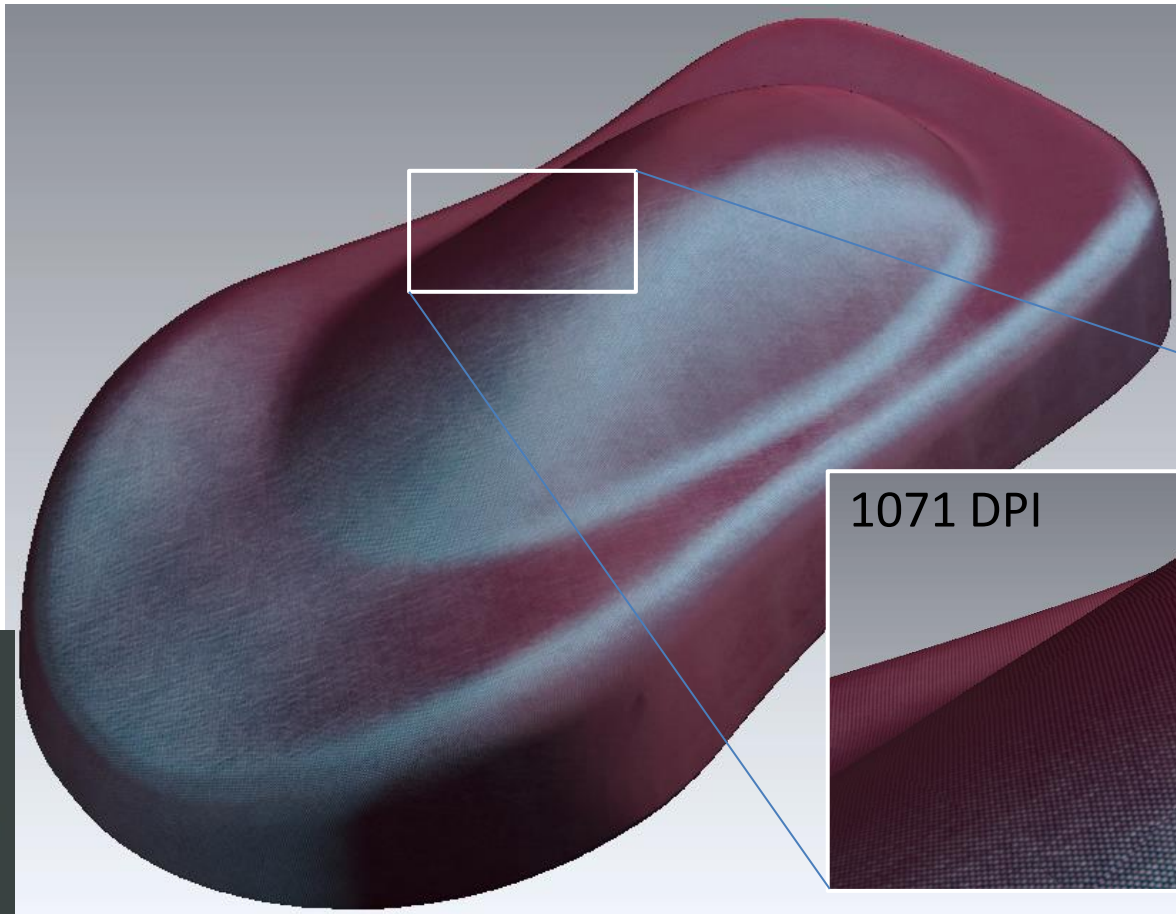
polyester fabric



BRDF



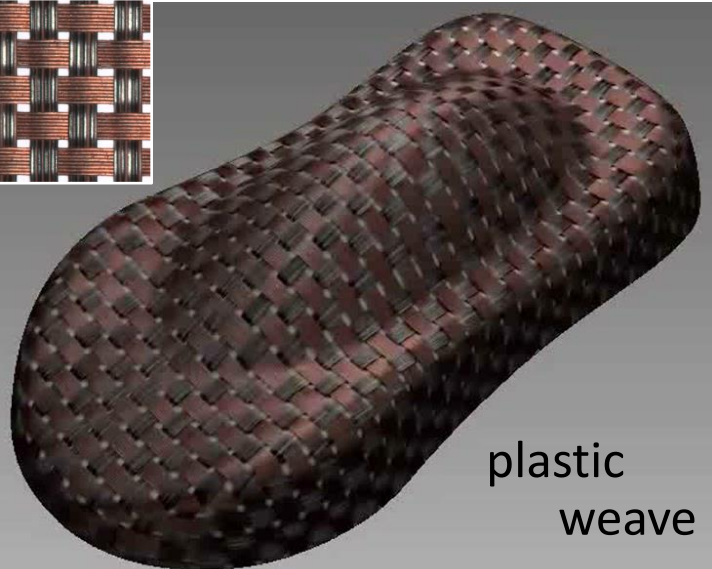
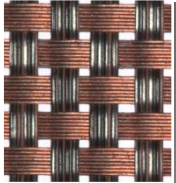
BTF – additional texture information



1071 DPI



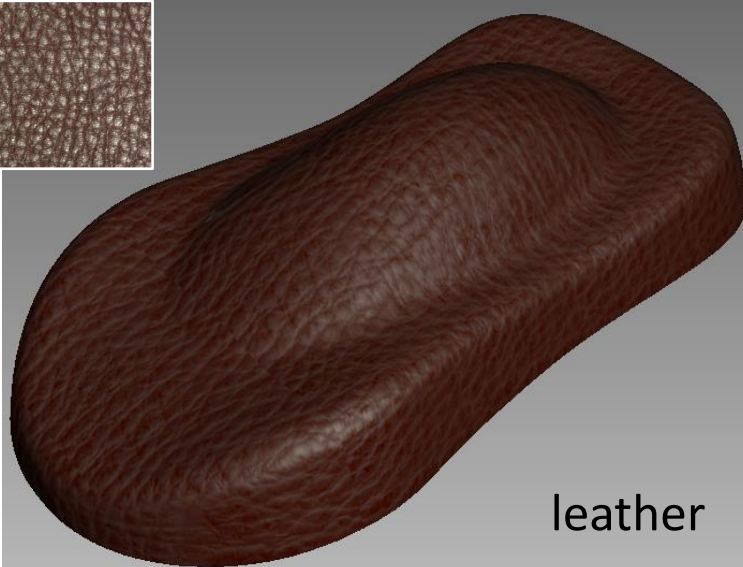
# Measured BTF Data



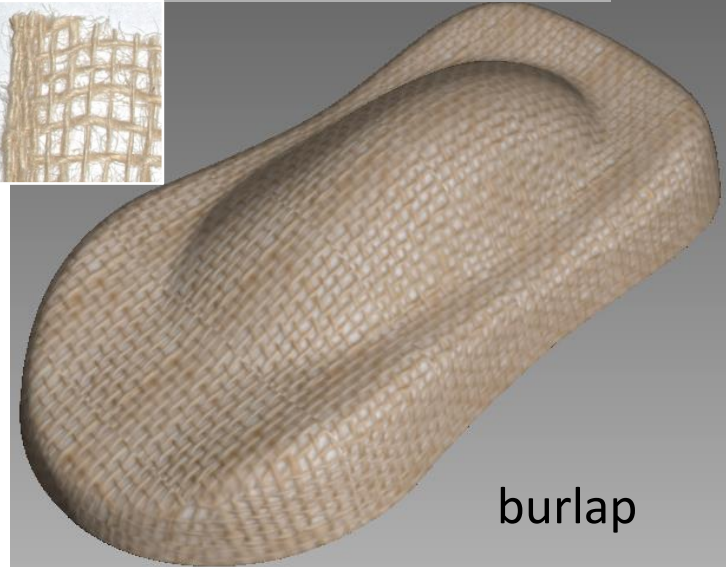
plastic  
weave



wood



leather



burlap

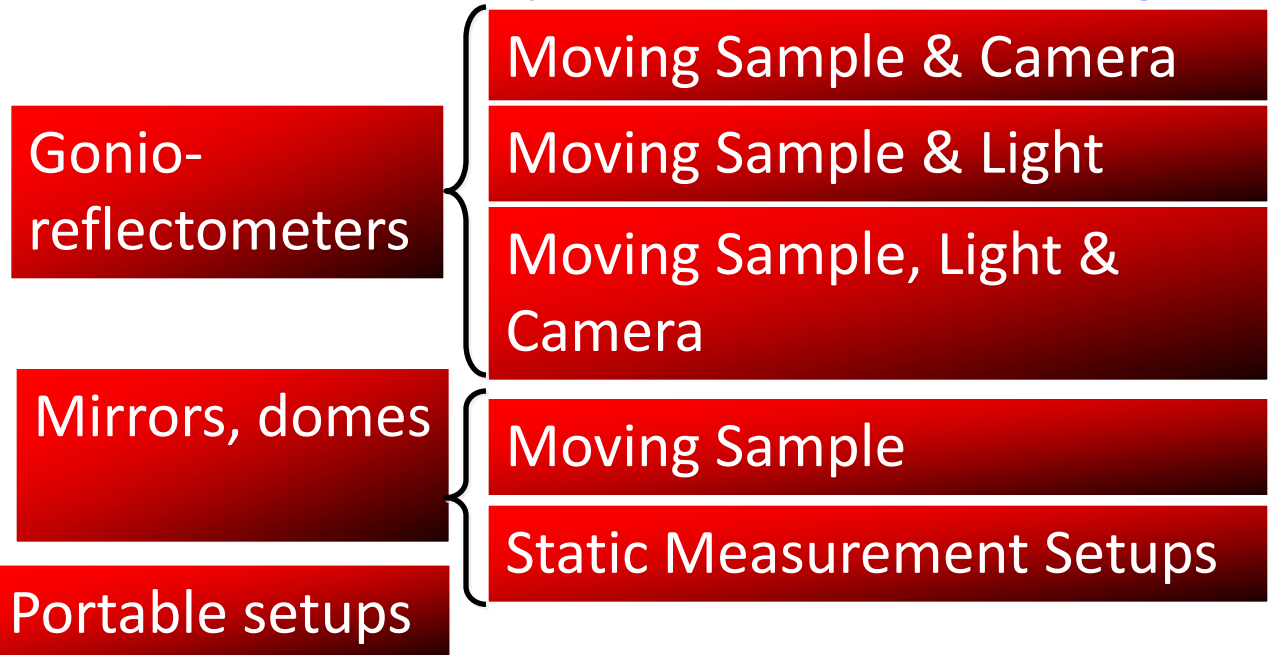
# BTF Measurement Setups Taxonomy



$$BTF(\lambda, x, y, \theta_i, \varphi_i, \theta_v, \varphi_v)$$

**7 dimensional data**  $\Leftrightarrow$   
 4 dimensions depend on camera, light & sample positioning

Measurement setup with **4 mechanical degrees of freedom**:



sample/camera **3/1** (1/1 + many lights)  
 sample/light **2/2**  
 sample/light/camera **1/2/1**  
 sample **1** + many lights & cameras  
 many lights & cameras (real/virtual)

# BTF Sample Acquisition

1999

Gonioreflectometer – Moving Sample & Camera

CURET-Columbia&Utrecht  
University  
[Dana et al. ACM TOG99]

Database: **61 samples**

Illu./View directions:

**55/max.205 = 215 img.**

Max. illu./view elev.:

**85°/85°**

Rectified images:

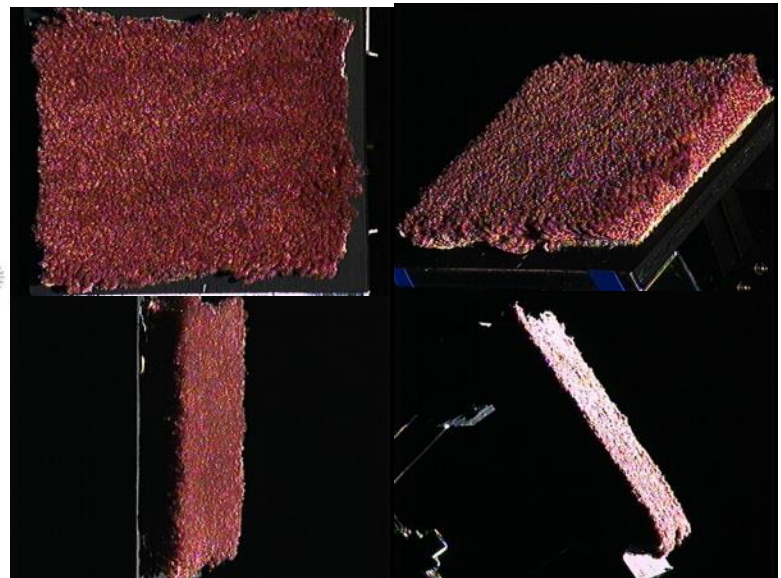
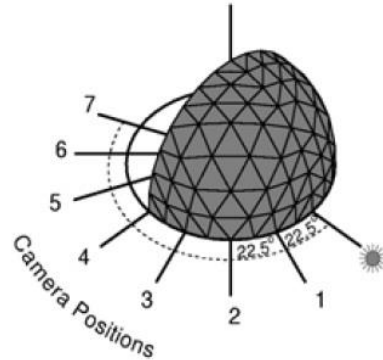
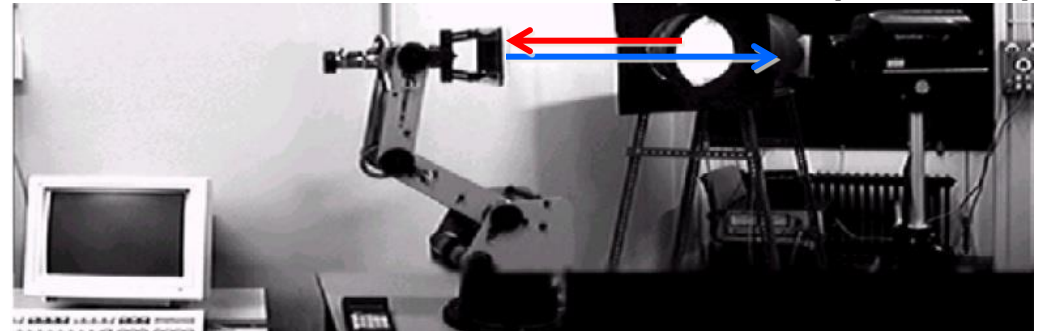
**400 x 300 pixels**

Measurement time:

**n/a**

<http://www1.cs.columbia.edu/CAVE/software/curet>

[Dana et al. 99]



# BTF Sample Acquisition

2003

## Gonioreflectometer – Moving Sample & Camera

Bonn University

[Sattler et al. EGSR 03]

Database:

10 samples (4 HDR)

Illu./View directions:

81/81 = 6 561 img.

Max. illu./view elev.:

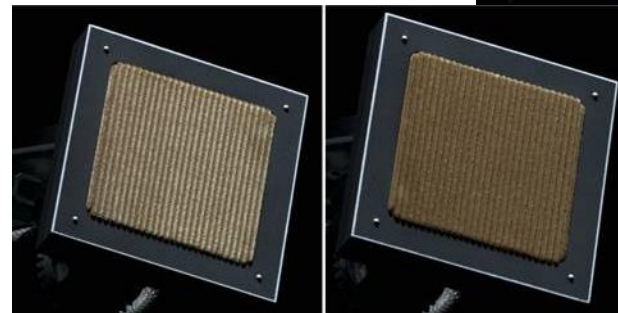
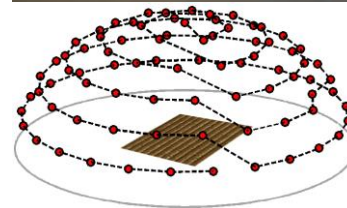
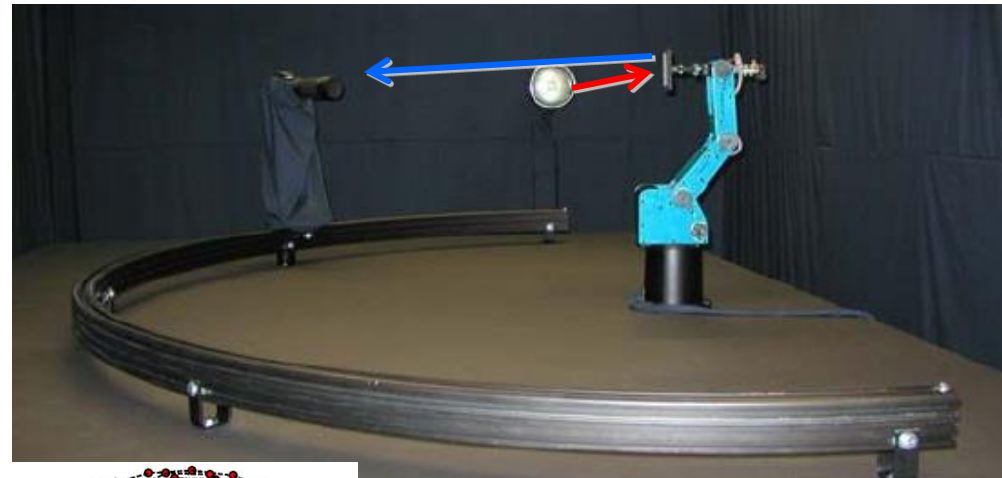
75°/75°

Rectified images:

800 x 800 pixels

Measurement time:

~ 14 hours



[Sattler et al. 03]

# BTF Sample Acquisition

2003

Gonioreflectometer – Moving Sample & Light

Yale University [Koudelka et al., TEXTURE 03]

Database: **17 samples**

Illu./View directions:

**120/90 = 10 800 img.**

Max. illu./view elev.:

**80°/75°**

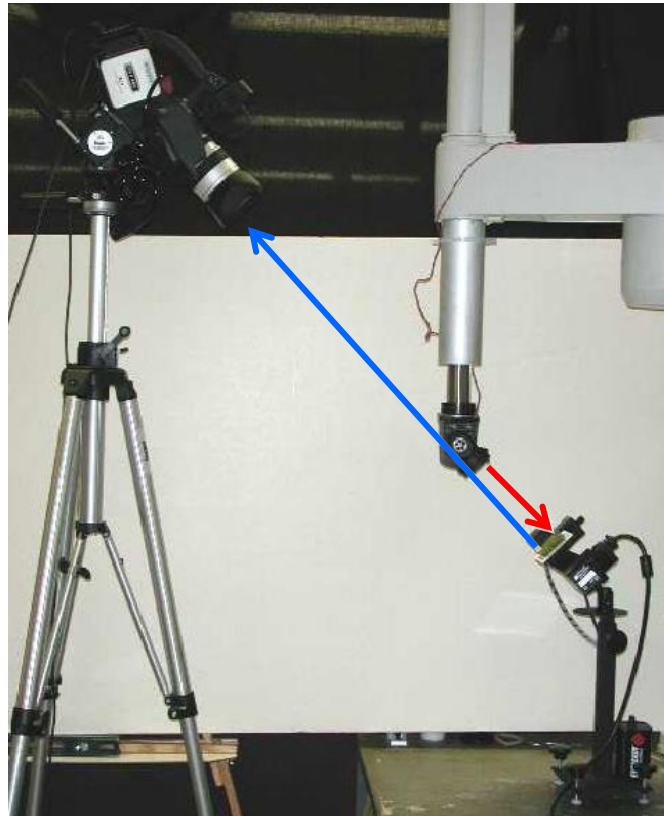
Rectified images:

**192 x 192 pixels**

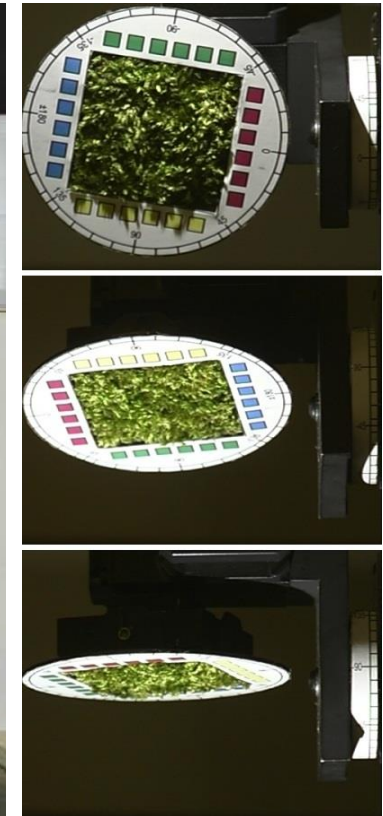
Measurement time:

**~ 10 hours**

<http://vision.ucsd.edu/kriegman-grp/research/vst>



[Koudelka et al. 03]



# BTF Sample Acquisition

Gonioreflectometer – Moving Sample, Light & Camera

UTIA AS CR  
[Haindl&Filip CVPR13]

Illu./View directions:  
arbitrary/arbitrary (81/81)

Max. illu./view elev.:  
90°/90°

Rectified images:

2000 x 2000 pixels

Database: publicly available

Measurement time: ~10 hours

<http://btf.utia.cas.cz>



- Spectral & HDRI measurements
- Arms angular accuracy: 0.03°
- Resolution: over 1000 DPI



# BTF Sample Acquisition

2004

## Mirrors – Moving Sample & Light

Rutgers University  
[Dana & Wang, JOSA 04]

Database: n/a

Illu./View directions:

continuous

Max. illu./view elev.:

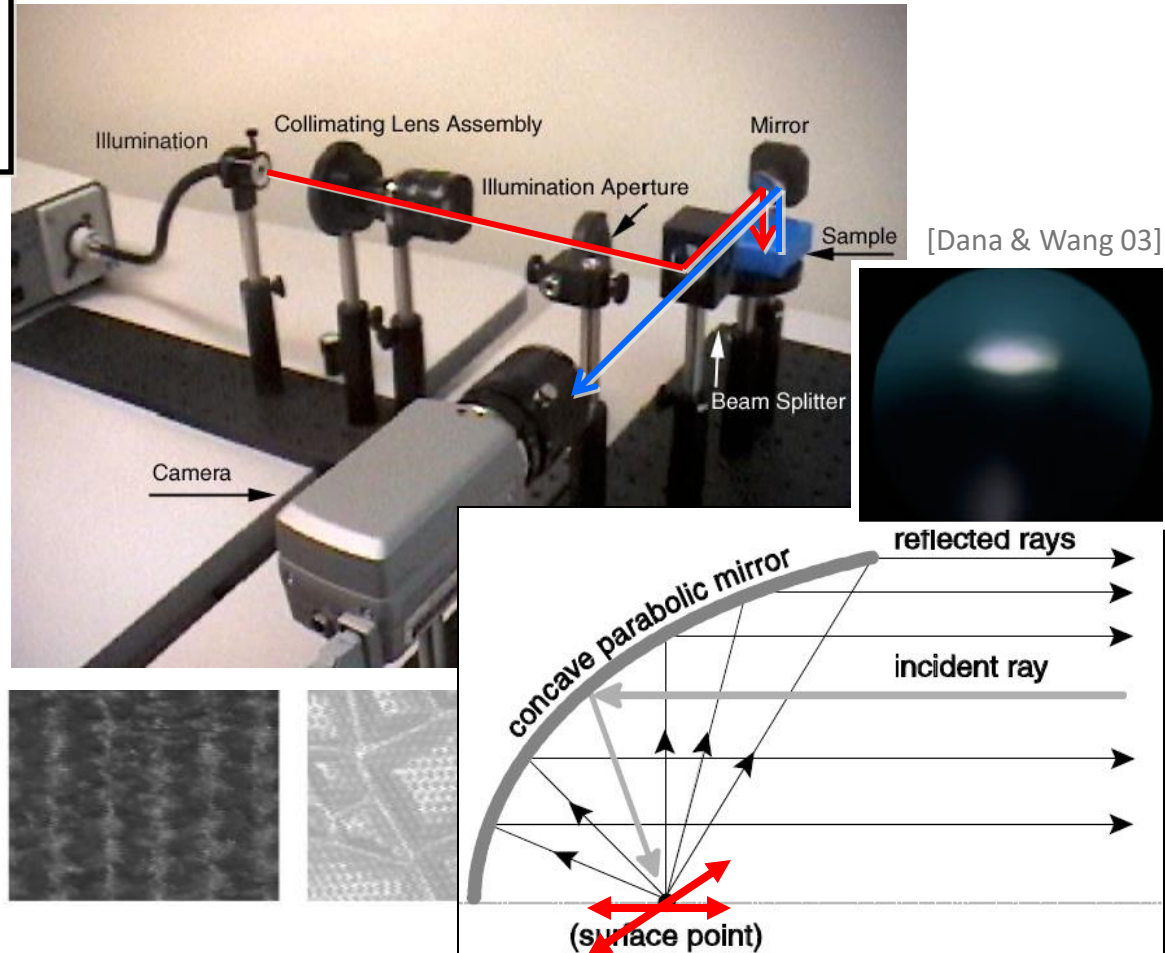
23-37°/23-37°

Rectified images:

~ 200 x 200 pixels

Measurement time:

~1 hour



[Dana & Wang 03]

Material moves below mirror

## Mirrors – Static Measurement Setups

**New York University**  
**[Han et al., ACM TOG 03]**

Database: n/a

Illu./View directions:

22-79/22-79 =

484 – 6241 img.

Max. illu./view elev.:

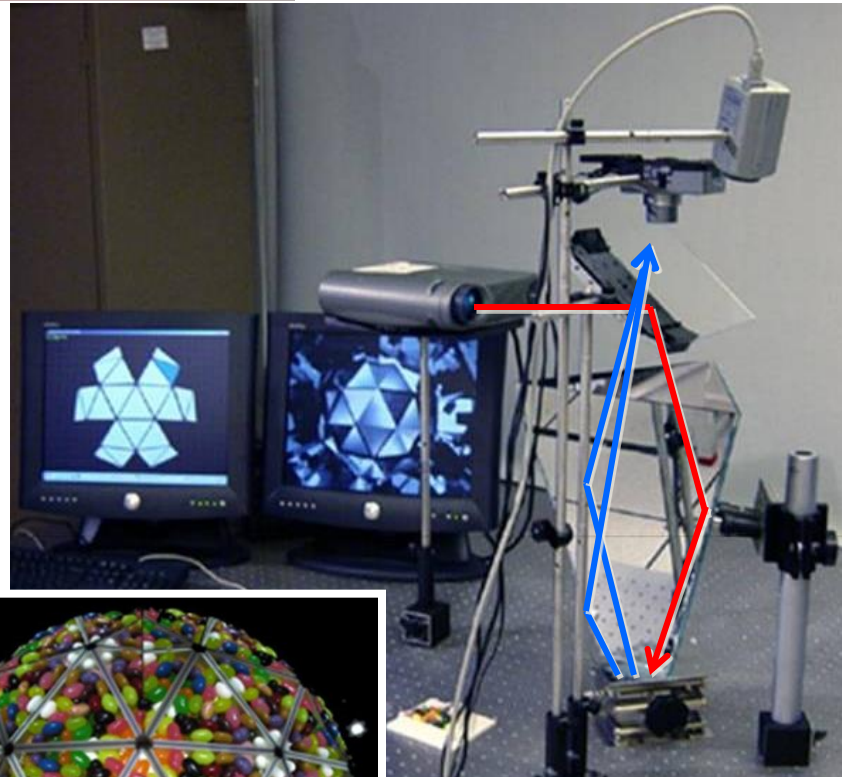
76°/76°

Rectified images:

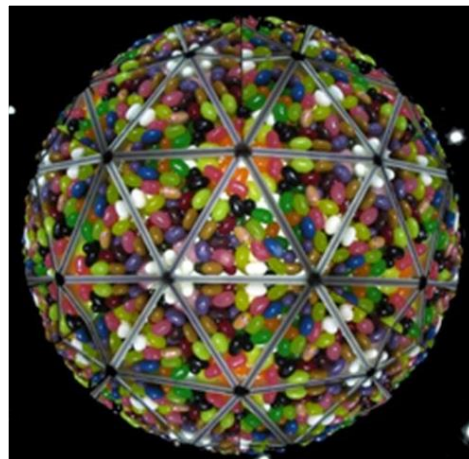
~ 200 x 200 pixels

Measurement time:

~1 hour



[Han et al. 03]



# BTF Sample Acquisition

2005

## Dome – Static Measurement Setups

**Bonn University**  
[Müller et al. 05]

Illu./View directions:

151/151 = 22 801 img.

Max. illu./view elev.:

n/a

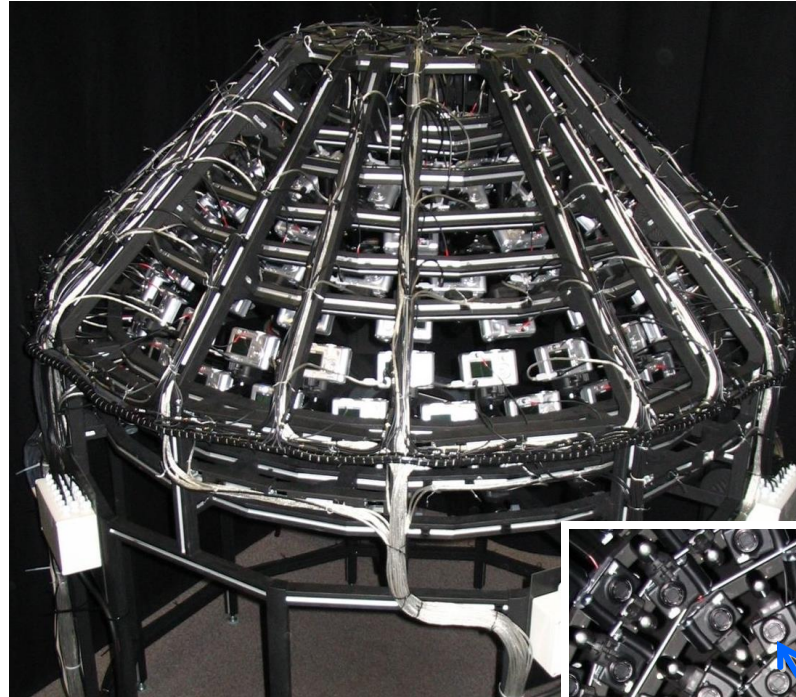
Rectified images:

1024 x 1024 pixels

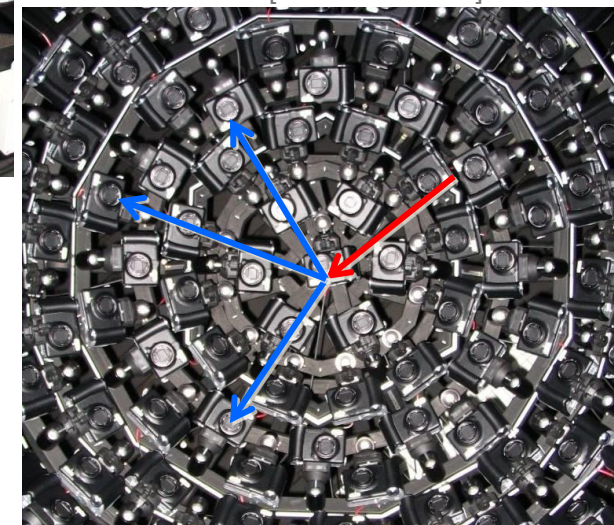
Database: n/a

Measurement time:

~1 hour



[Muller et al. 03]



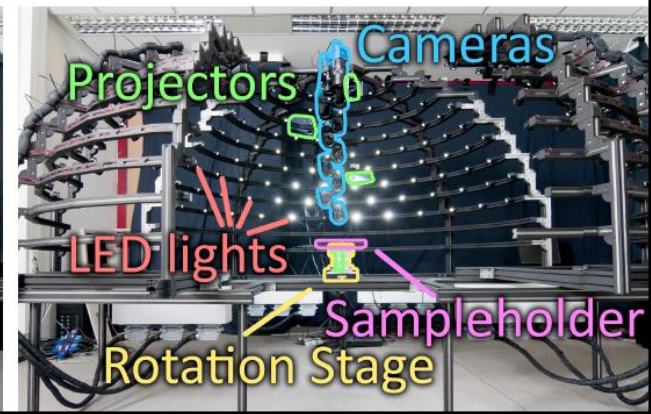
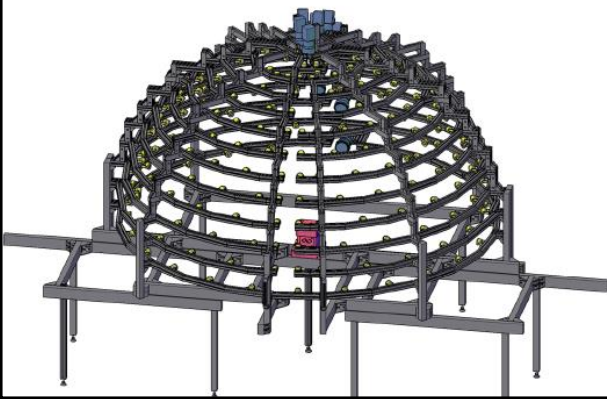
# BTF Sample Acquisition

2014

Dome – Moving Sample, portable

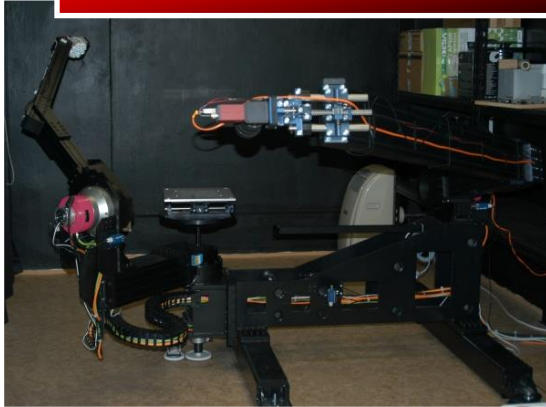
**Bonn University**  
[Schwartz et al. 14]

- Dome setup used in industry
- Illu./View directions: 198/264 = 52 272 images  
Max. illu./view elev.: 75 degrees  
Rectified images: 1024 x 1024 pixels  
Measurement time: 4-10 hours

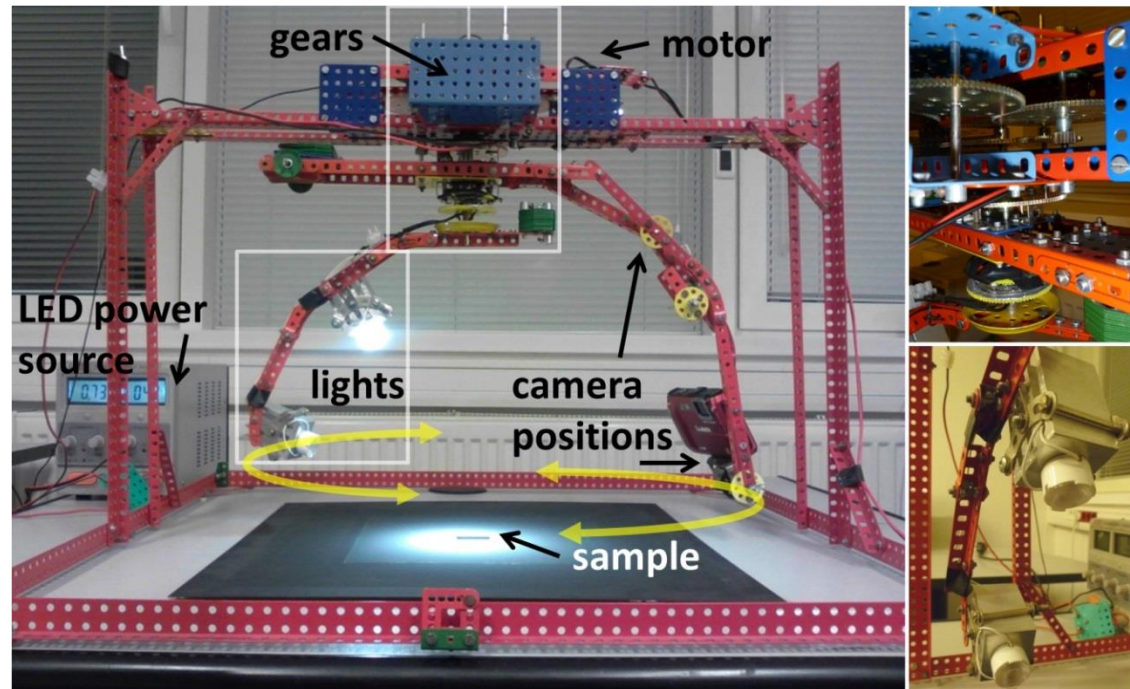


# Rapid Measurement Approach

## Portable Setups



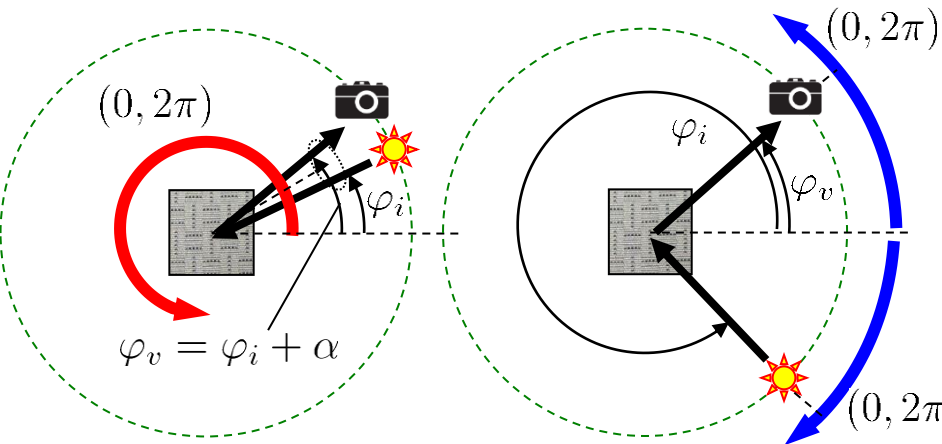
- Measurement of BTF 6561 images  $\Rightarrow$  20 hours
- **Faster solutions needed for practical usage**
- Proof-of-concept prototype  $\Rightarrow$  construction set



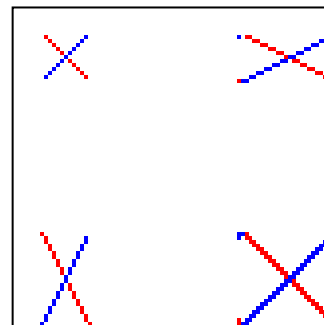
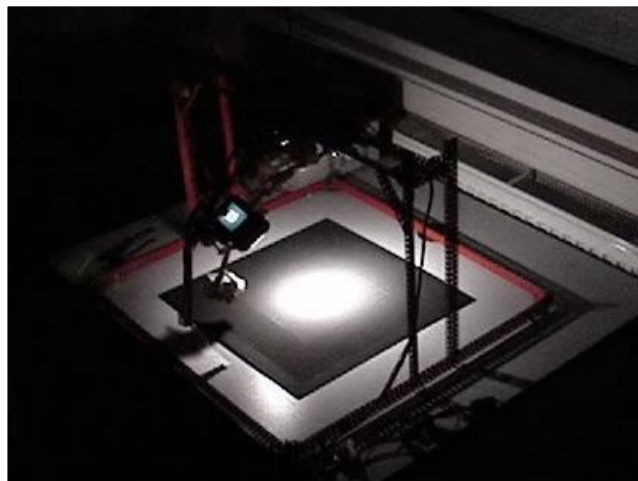
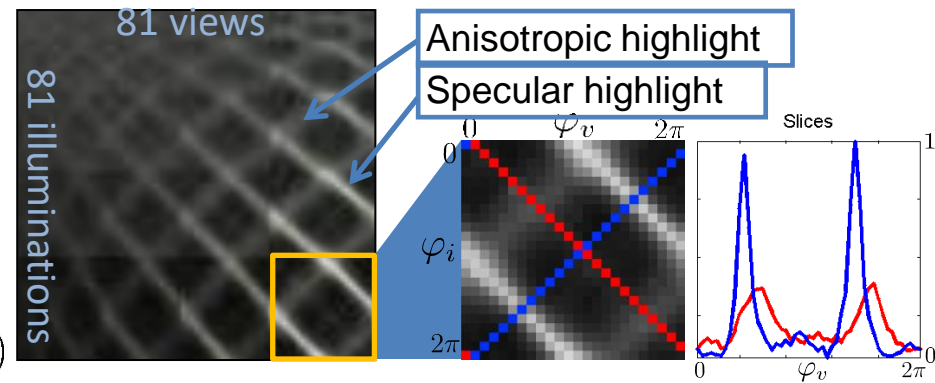
- 2 LEDs
- compact camera
- approximate BTF  $\Rightarrow$  capturing time 4 minutes

# Rapid Measurement Approach

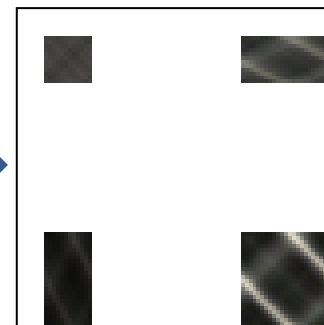
measurement procedure



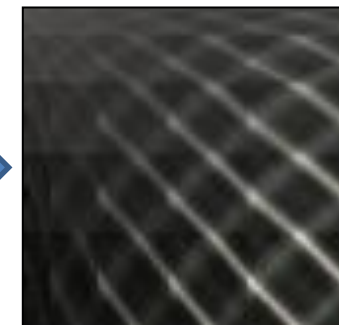
Reference <sup>6561</sup> images



8 slices 169  
images



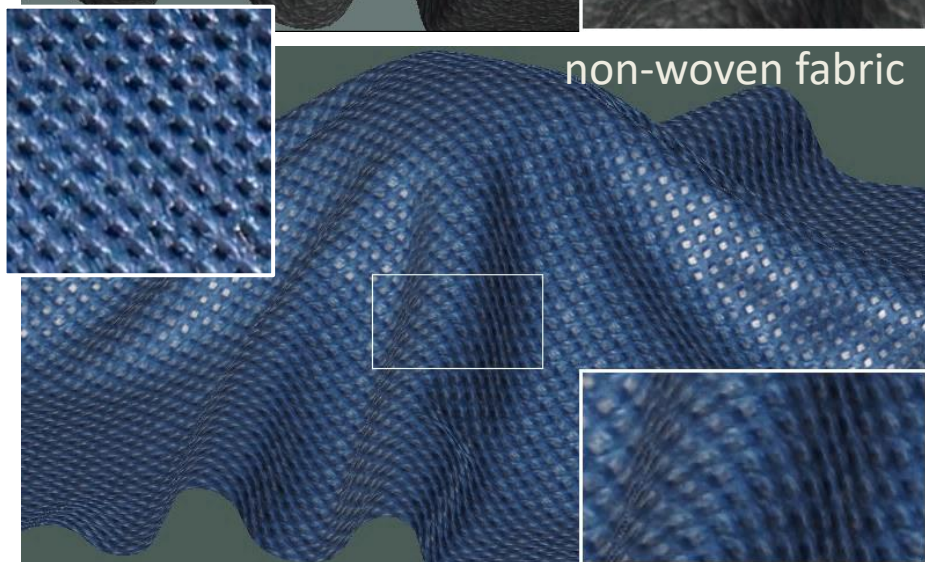
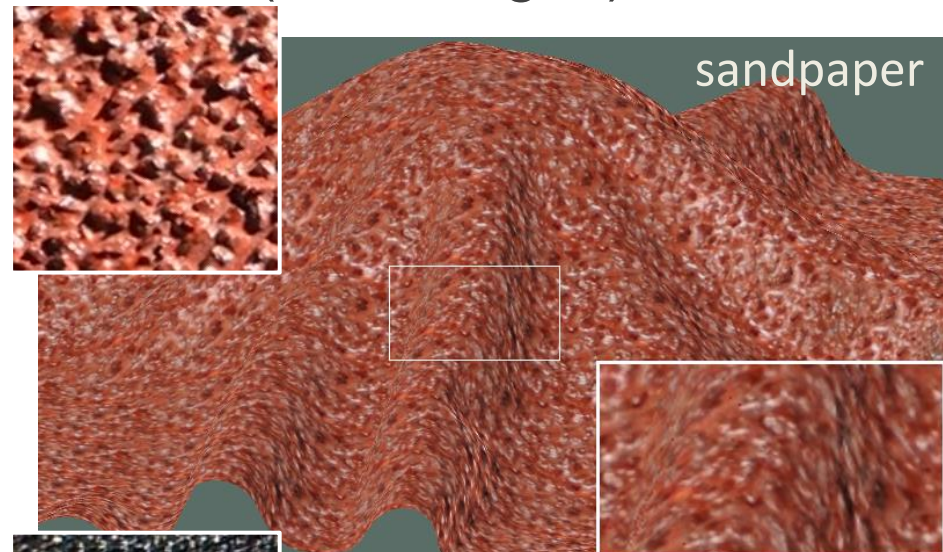
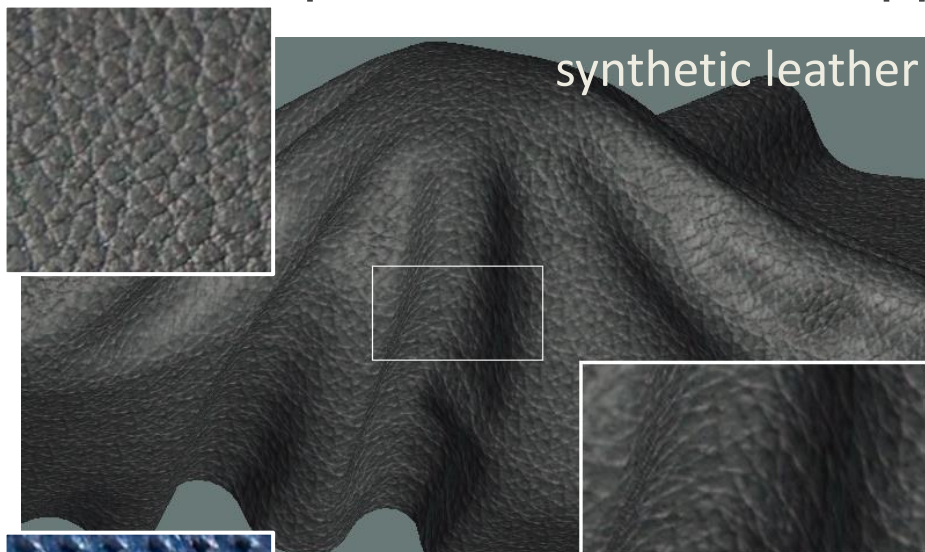
subspaces  
reconstruction



missing images  
interpolation

# Results of Portable Setup

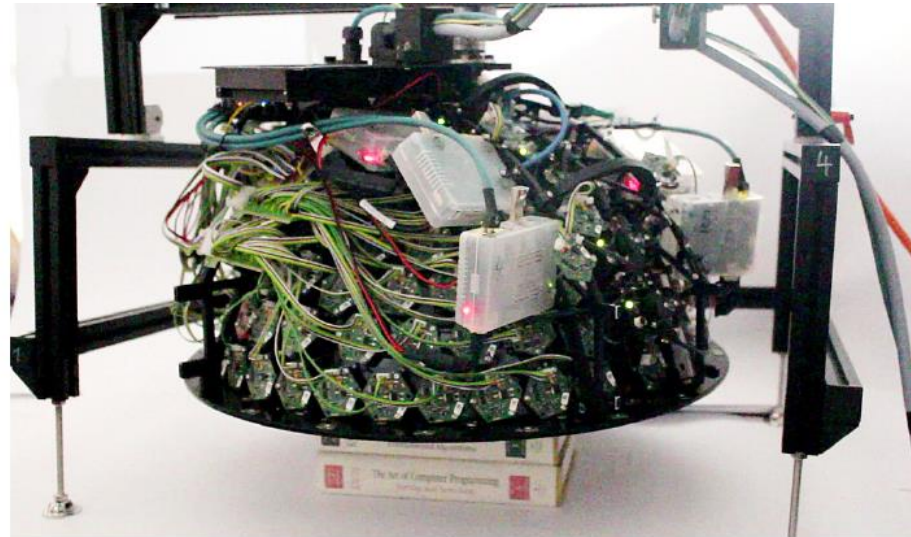
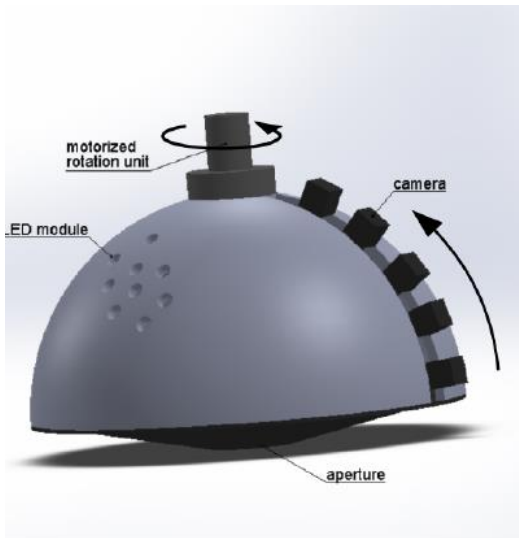
materials photo & measured appearance (169 images)



# Rapid Measurement Approach

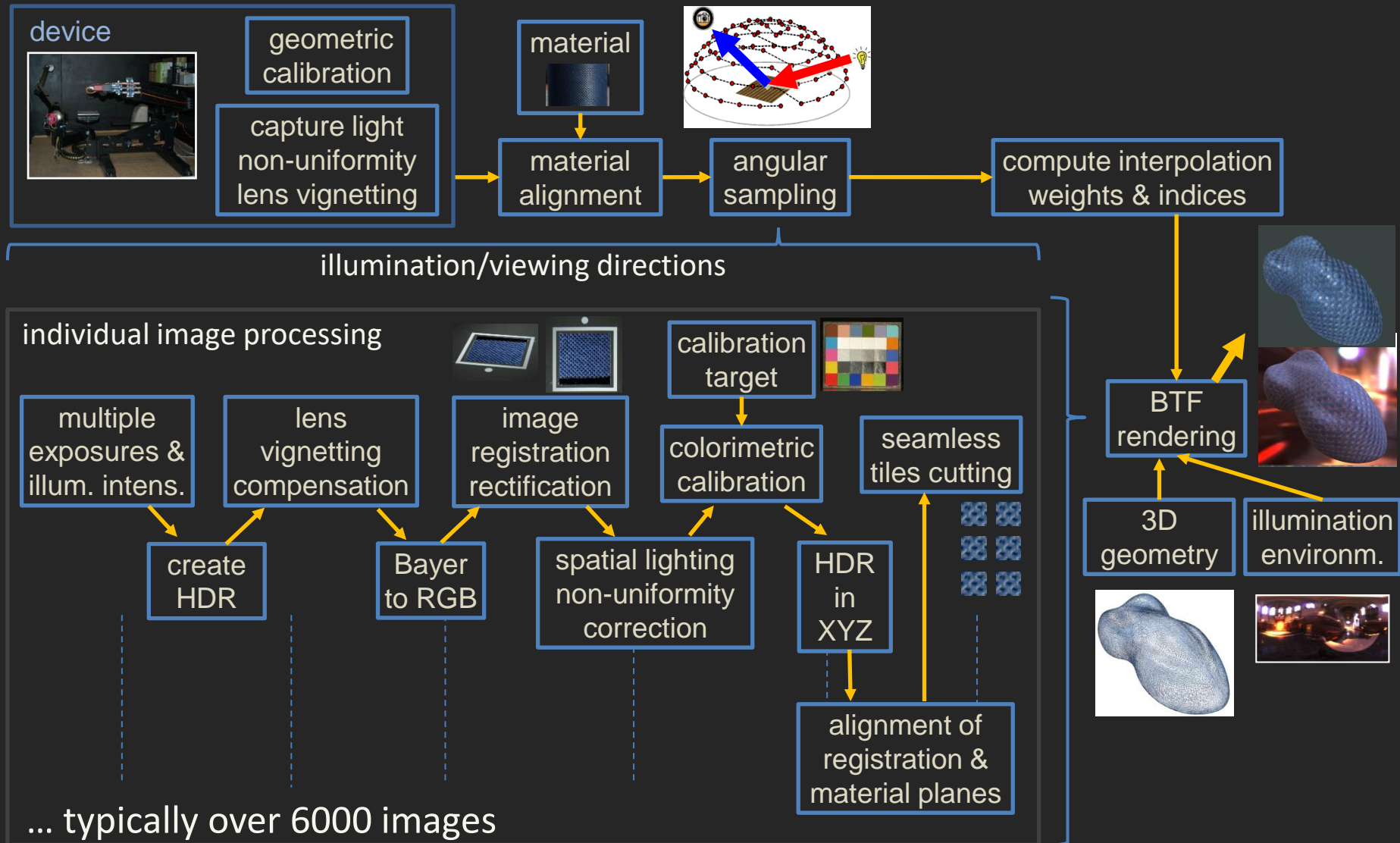
## Portable Setups

- **LightDrum** [Havran et al. Sensors 2016]
- Portable solution for fast on-site BTF measurement
- Body with lights and cameras rotates above the measured material





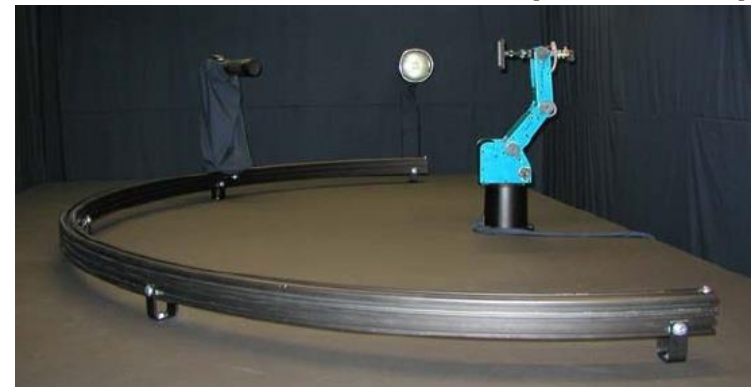
# BTF Capturing & Visualization Pipeline



# BTF – HDR and Spectral Measurement

- Most system measure RGB data in 8-bit/colour channel
- University Bonn Database (UBO) – 4 HDR architectural samples
- Materials appearance depends on light's spectrum  $\Leftrightarrow$  need for full spectral measurements.
- [\[Lyssi 09\]](#) – full spectral BTF measurement and calibration on [\[Sattler et al. 03\]](#) setup.
  - Spectral Filter  $\Leftrightarrow$  30 wavelength bands (430 – 720 nm)
  - 30 x 81 x 81 images  $\Leftrightarrow$  enormous measurement times (3 days)
  - sample in OpenEXR = **1 TeraByte**
- [\[Rump et al. 10\]](#) – GT data for multispectral BTF

[Sattler et al. 03]



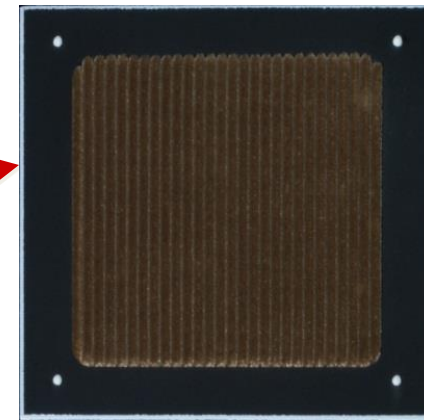
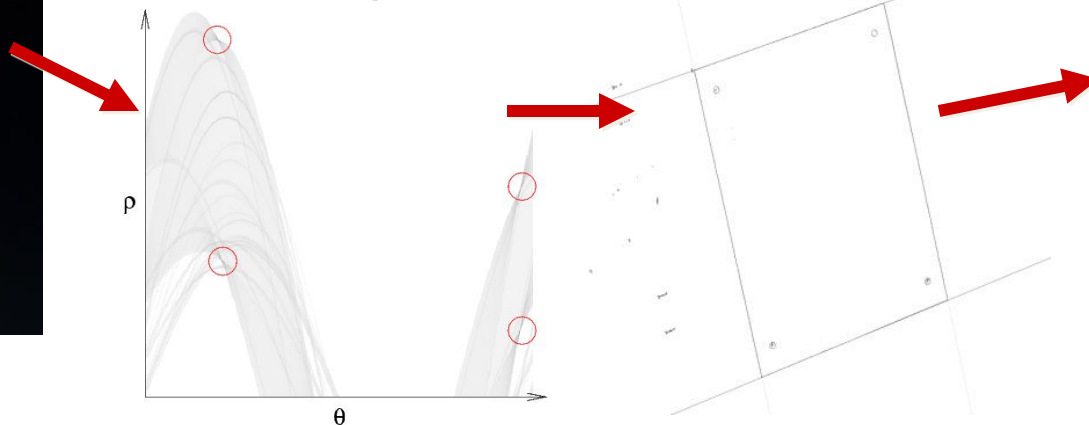
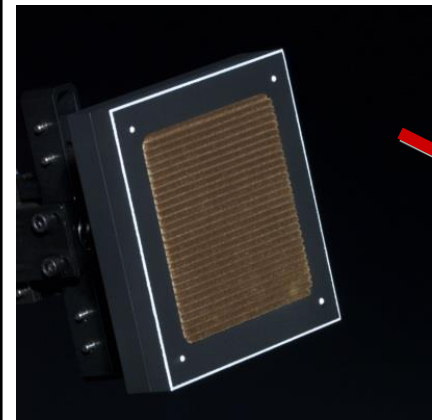
# Spatial Reflectance Data Rectification

- **Registration and resampling** images of different views  $\Leftrightarrow$  same size images, surface normal aligned with viewing direction

Using:

- Registration marks
- Intersection of sample borders
- Predefined geometric transformation (static setups)

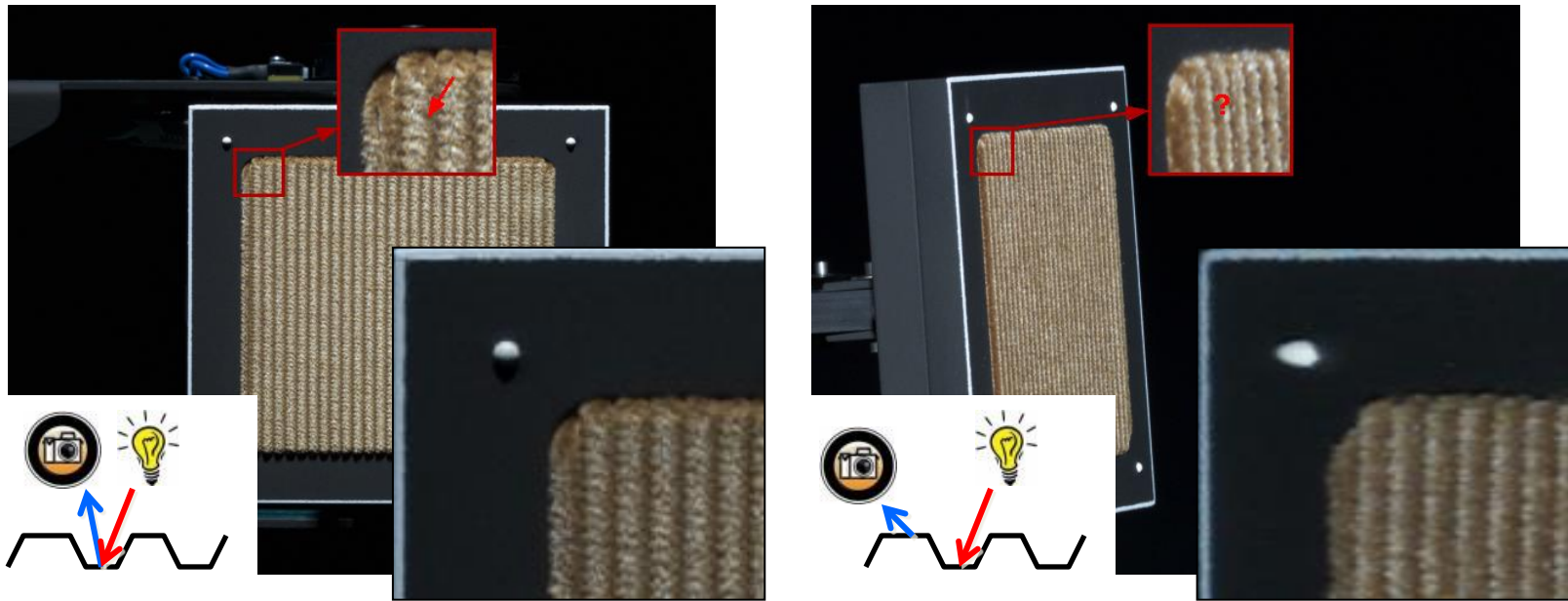
Lines detection  
Hough transform



# BTF vs. SV-BRDF

Contrary to SVBRDF, BTF face problem with rough structure samples

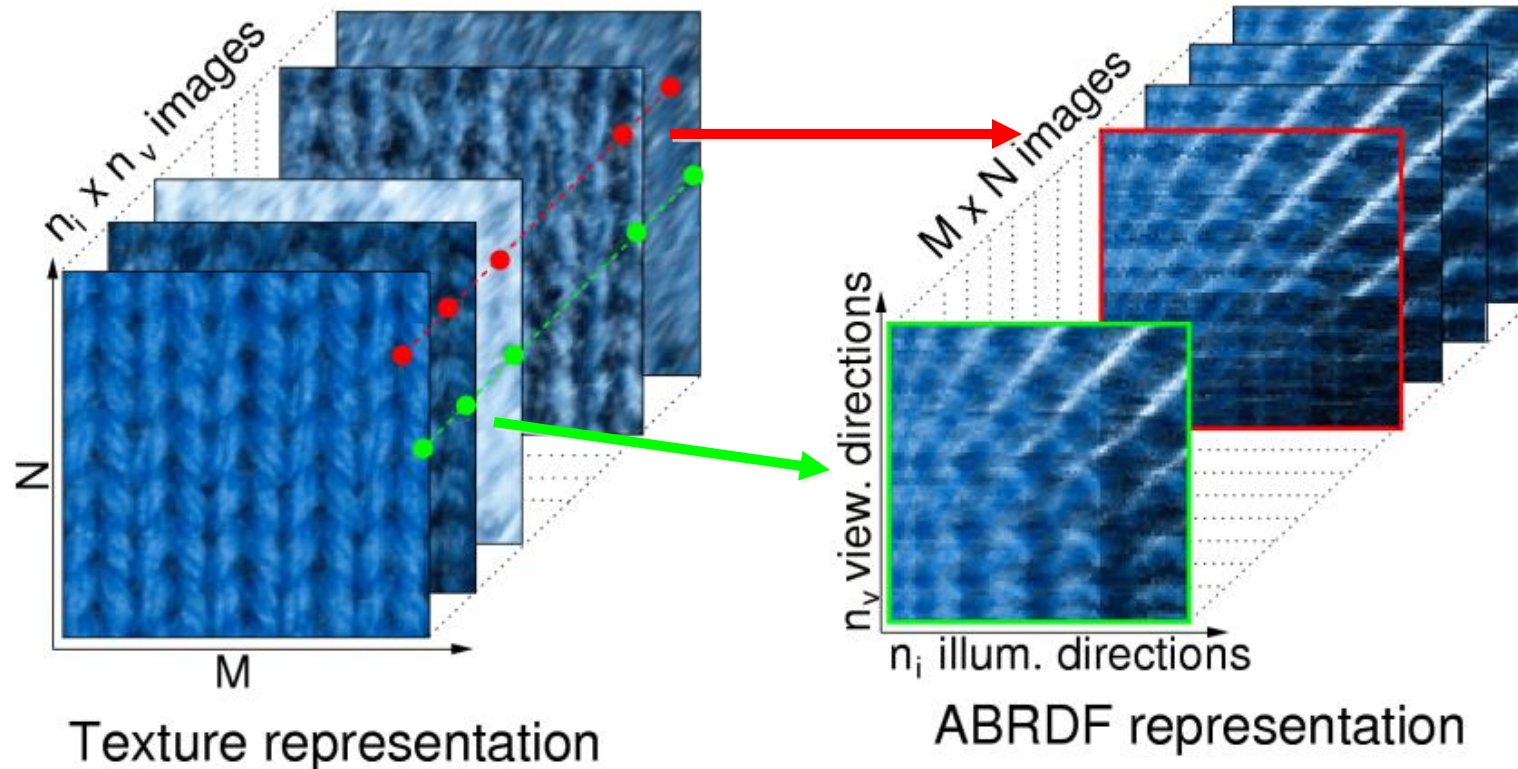
- Different views  $\Rightarrow$  **Pixel-wise misalignment**, due to occlusion
- Solution  $\Rightarrow$  process individual views separately



Courtesy of University of Bonn

BTF - no geometrical information  $\Rightarrow$  no material profile at object edges

# Measured Data Representation



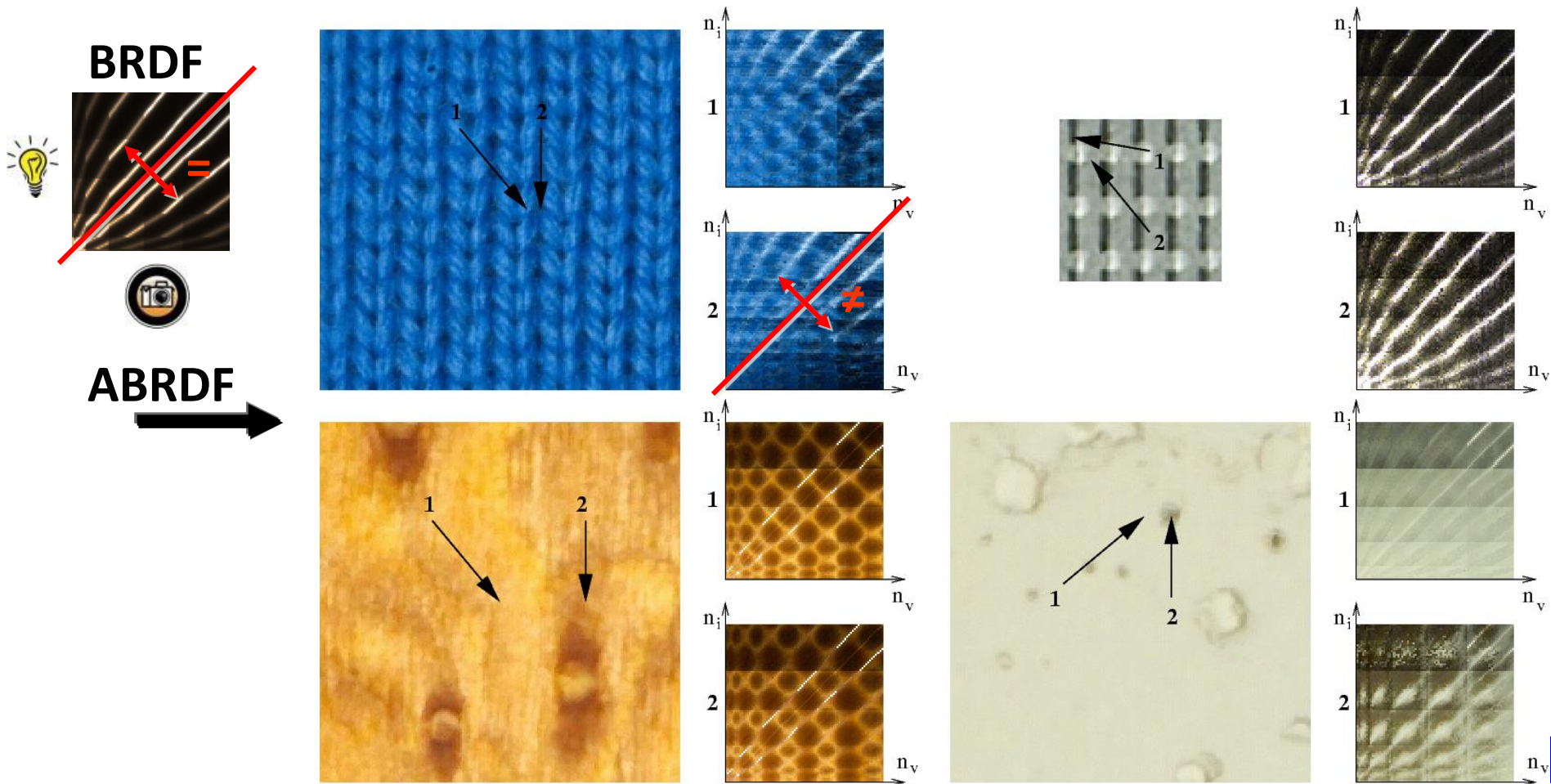
- Only images for the same view are correctly registered
- Shadows/occlusion compensation required prior to processing

- Illuminations/views aligned
- Highlights positions fixed
- Easier pixel-wise comparison.

# Apparent BRDFs

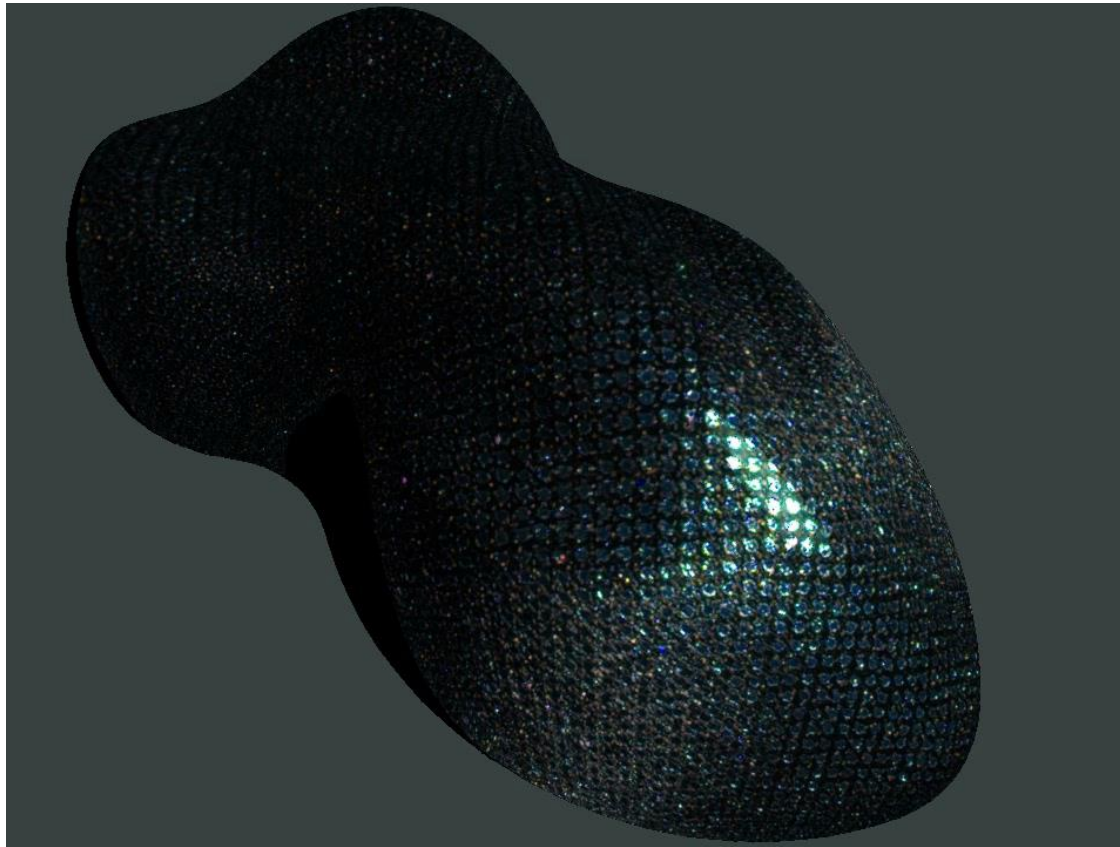
**Apparent BRDF  $\neq$  BRDF** (masking, occlusions, shadowing, etc.)

possible violation of: **Helmholtz reciprocity & energy conservation**

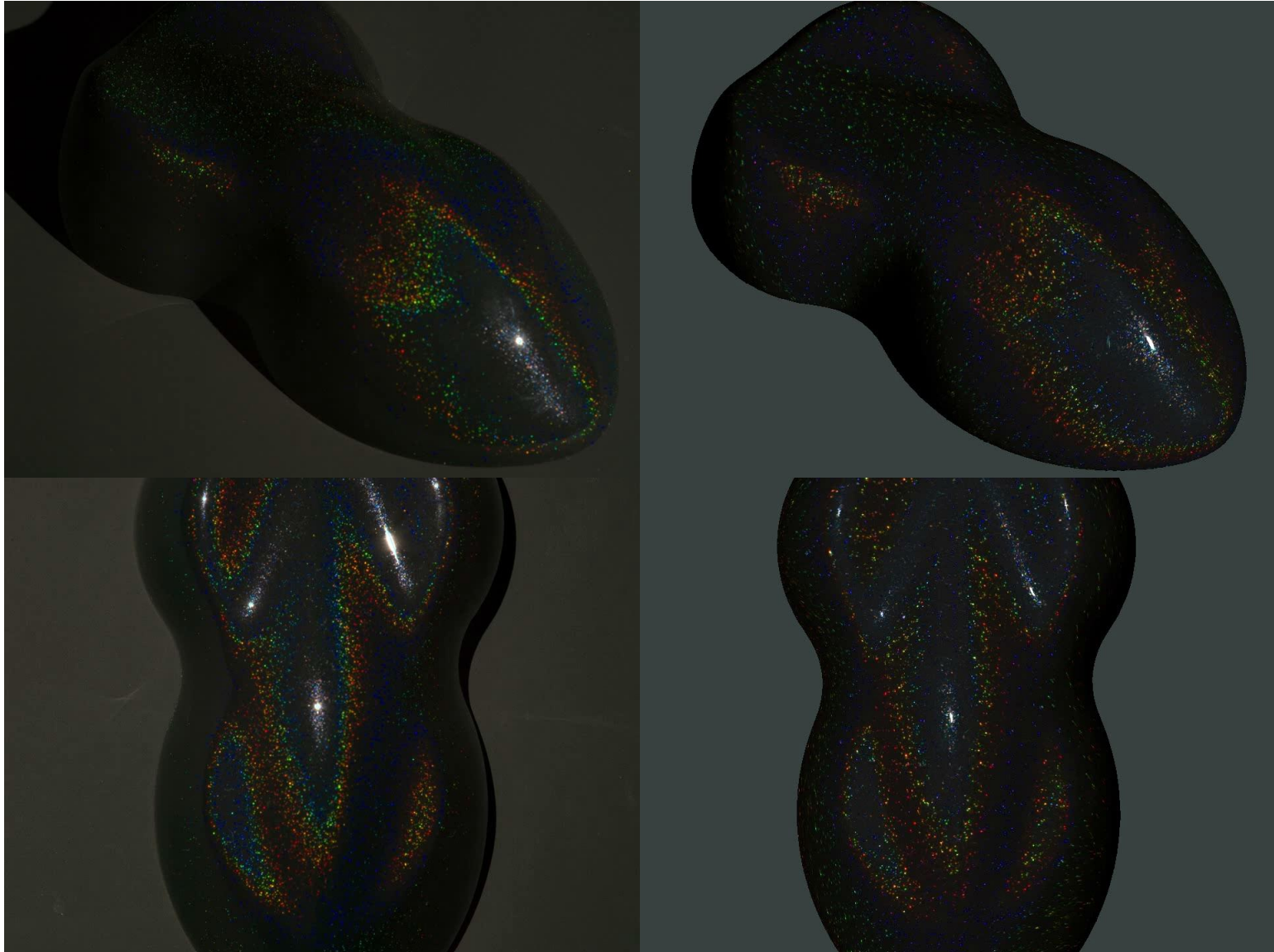


# Challenging materials

- Combination of specular, diffuse and anisotropic features



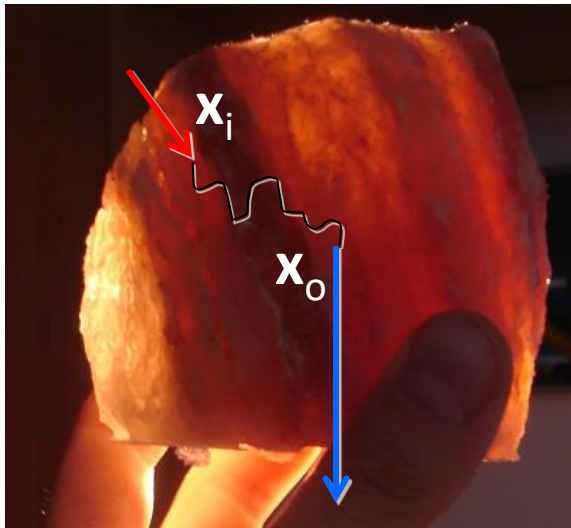
# Challenging materials





# BSSRDF Measurement

## Bidirectional subsurface-scattering reflectance distribution function



$$BSSRDF(\lambda, \underline{x_i}, \underline{y_i}, \underline{x_o}, \underline{y_o}, \underline{\theta_i}, \underline{\varphi_i}, \underline{\theta_o}, \underline{\varphi_o})$$

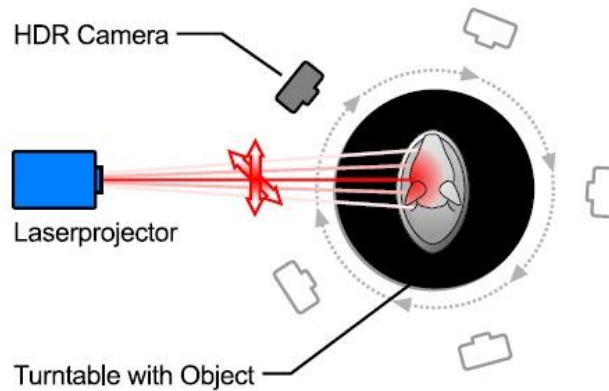
[Nicodemus et al. 77]

BTF includes scattering information,  
but difficult to separate

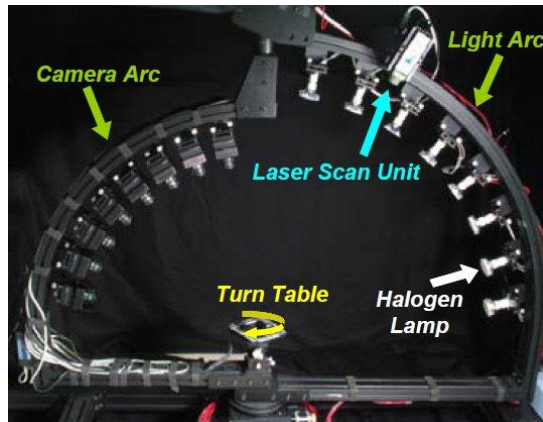
- **General 9 dimensional data**  $\Leftrightarrow$  often called as **reflectance fields**
- Describes light transport (scattering) in material structure between any pairs of incoming and outgoing rays
- Translucent materials
- Direct measurement very sparse due to high data dimensionality

# BSSRDF Measurement

**[Goesele et al. TOG 04]** – laser-based sparse spatially varying subsurface scattering measurement



**[Tong et al. TOG 05]** – BTF combined with local laser-based subsurface scattering measurement



BTF+local scat.

BTF

BTF+global scat.

# BSSRDF Measurement

- Models of subsurface scattering in homogeneous dielectric materials are available, measurement of models parameters: **[Jensen et al. SIG 01]** – dipole model of dielectrics, validated by scattering measurement of focused beam

Without  
scattering  
model



With  
scattering  
model

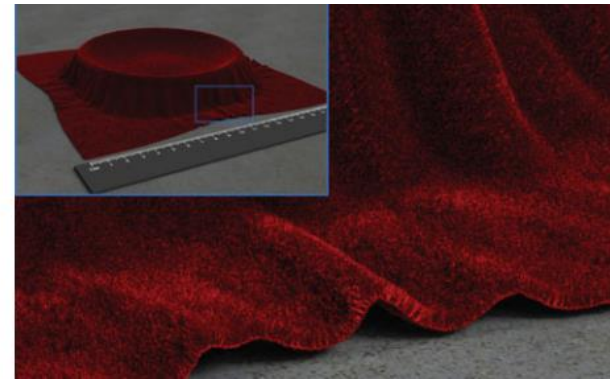
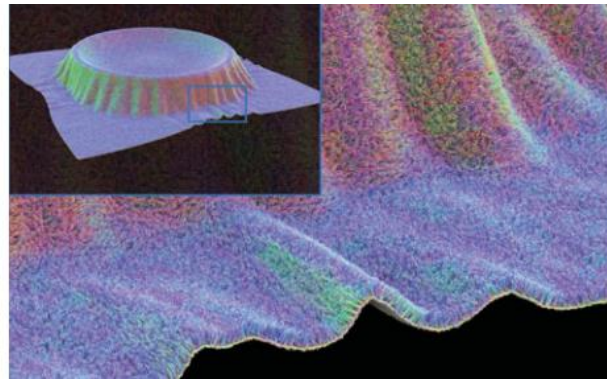
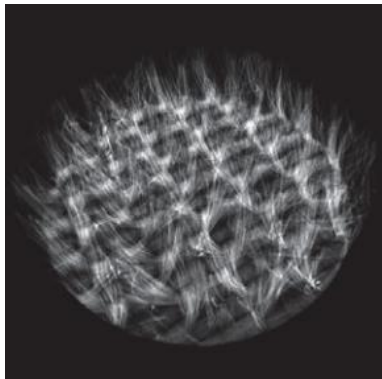


- Diffuse/specular reflectance components separation (polarization/color/illum. patterns) **[Shaffer 85]**, **[Nayar et al. JCV 97]**, **[Nayar et al. TOG 06]**  $\Leftrightarrow$  diffuse component represents light refraction inside material structure  $\Leftrightarrow$  fitting scattering models parameters to diffuse component.

# Volumetric Models Acquisition

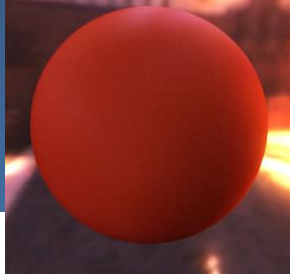
**[Zhao et al. 11 TOG]** – material geometry scanned by X-Ray Micro CT scanner (resolution  $1024^2$ ). Scattering information transferred to volumetric data by matching of several samples photographs.

- ✓ realistic appearance
- ✗ assumes single material, lengthy rendering, limited dynamic range of the scanner

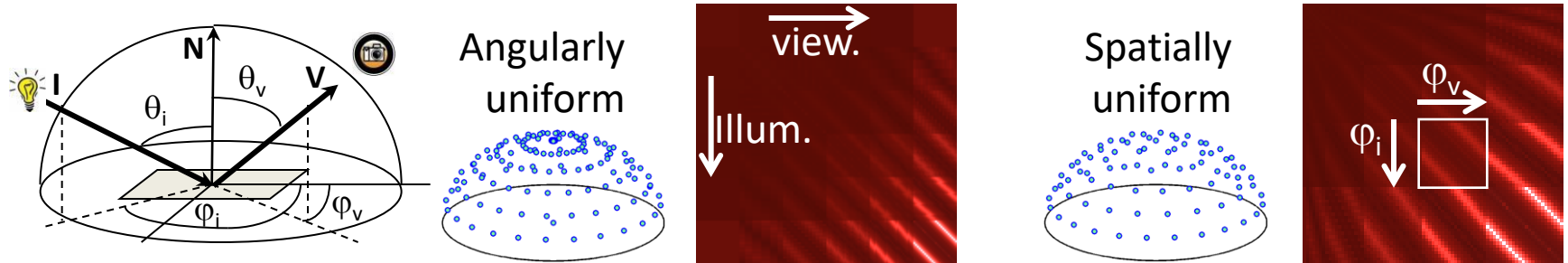


[Zhao et al. 11, ACM]

# Angular Parameterizations



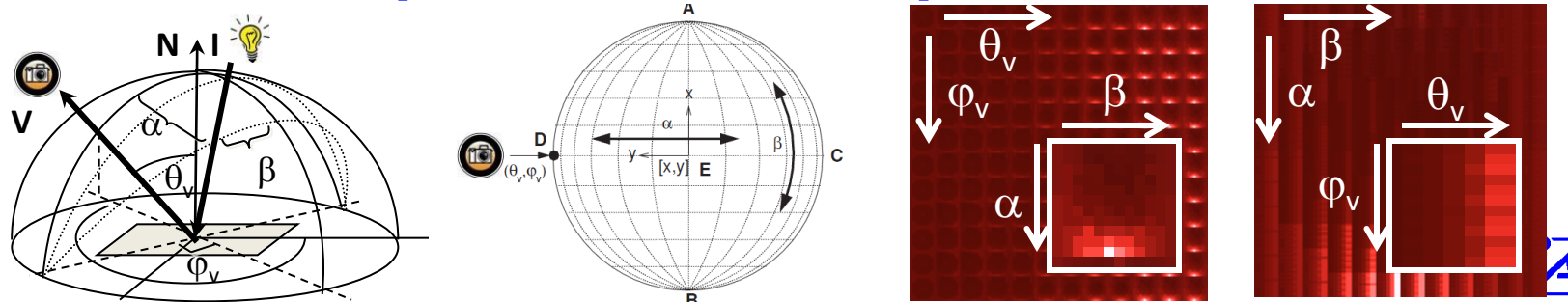
- Illumination-view



- Half-difference angles [Rusinkiewicz 98]

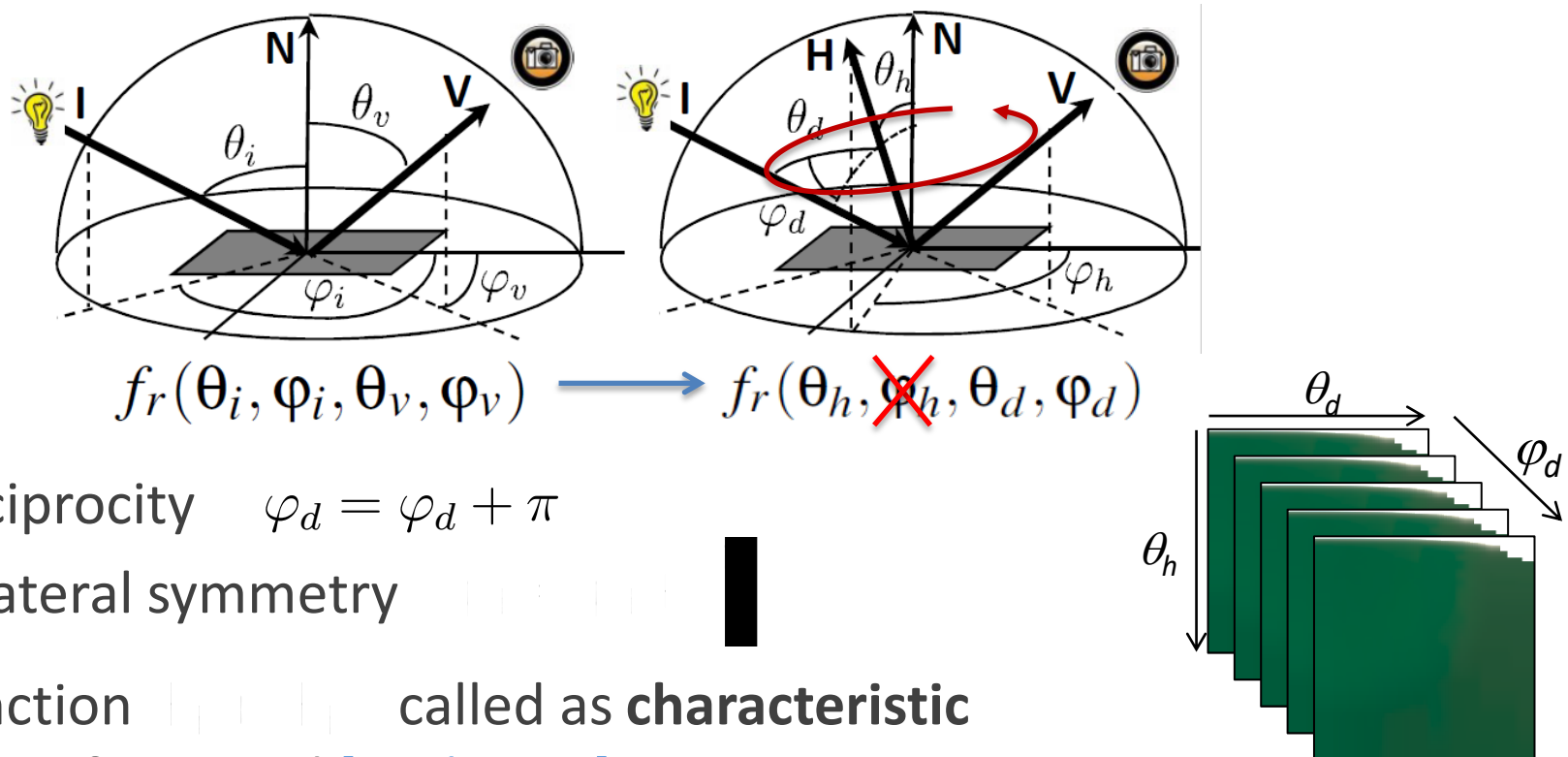


- Onion slices model [Havran et al. CGF 09]

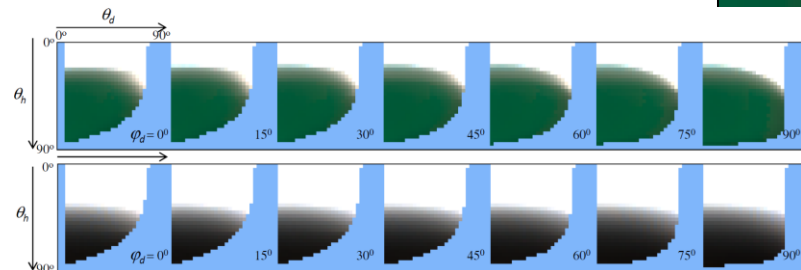


# Half-Difference Parameterization

BRDF in half-difference parameterization [Rusinkiewicz 98]



- reciprocity  $\varphi_d = \varphi_d + \pi$
- bilateral symmetry
- function called as **characteristic slice of material** [Burley 12]
- Bivariate BRDF



# Anisotropic Material Appearance

- property of being directionally dependent
- azimuthally-dependent material's appearance

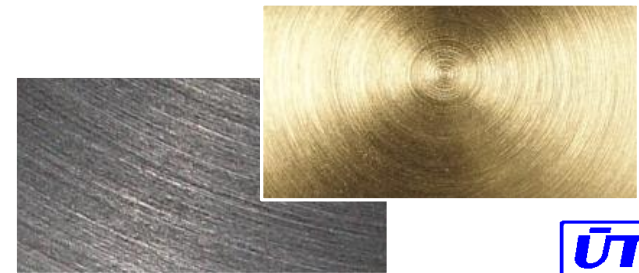
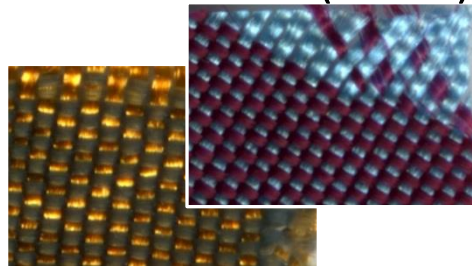
Present in many materials:



directional fibers  
(fabric, wood, hair)

weaving pattern/height profile  
of threads of fibers (fabric)

surface machining/finishing  
(metal, plastic, wood, ...)



# Anisotropic vs. Isotropic Appearance

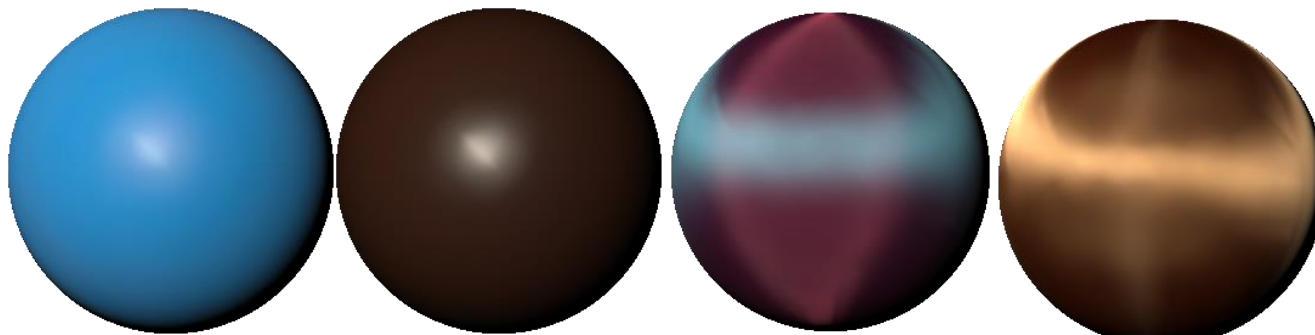
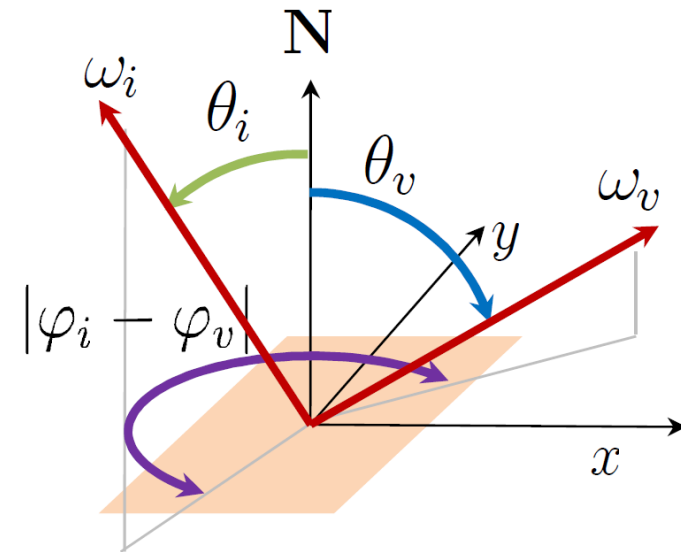
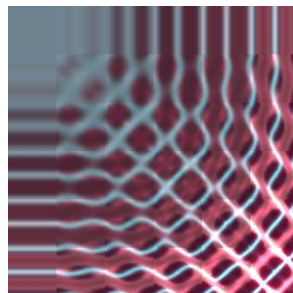
- BRDF – Bidirectional Reflectance Distribution Function
- Illumination and view dependent reflectance

$$BRDF(\lambda, \theta_i, \phi_i, \theta_v, \phi_v)$$

- Isotropic vs. anisotropic BRDF

$$B(\theta_i, \theta_v, |\varphi_i - \varphi_v|)$$

$$B(\theta_i, \varphi_i, \theta_v, \varphi_v)$$





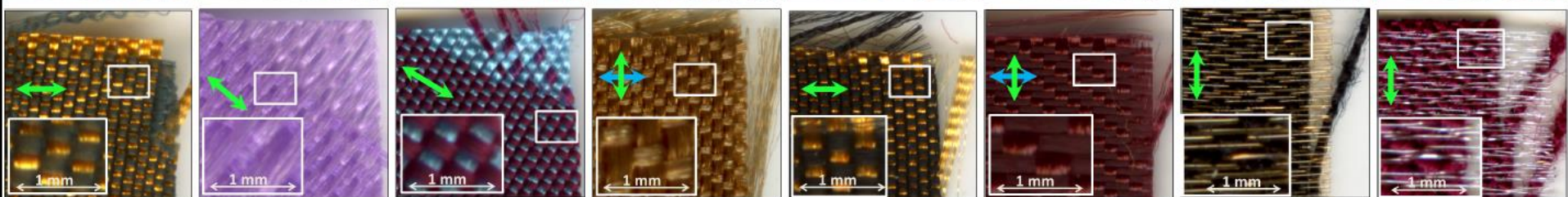
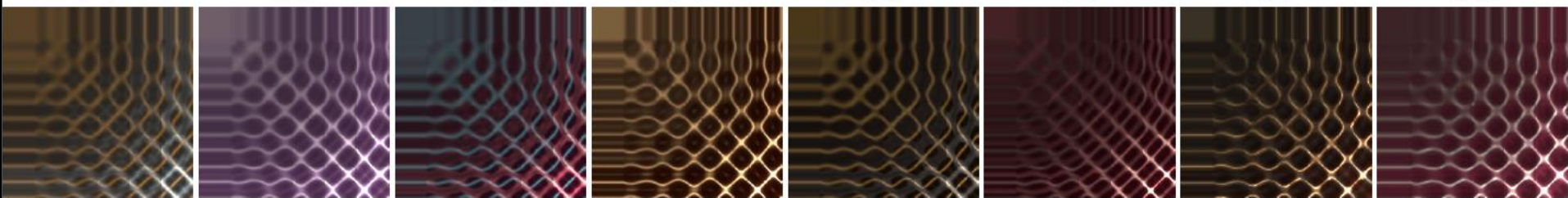
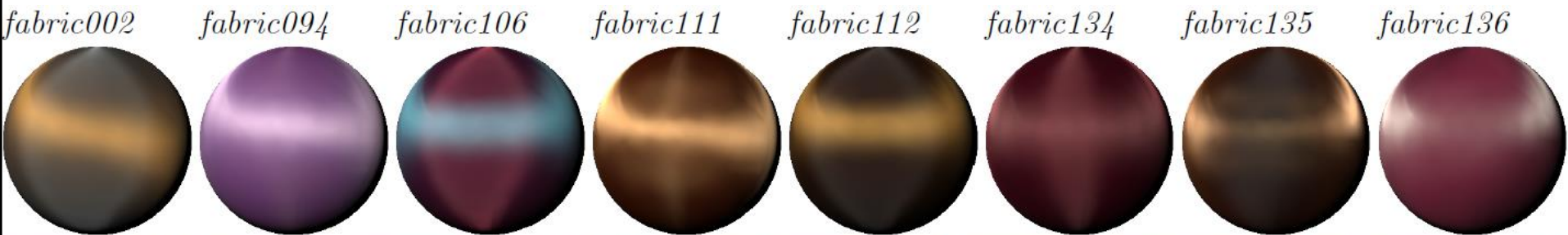
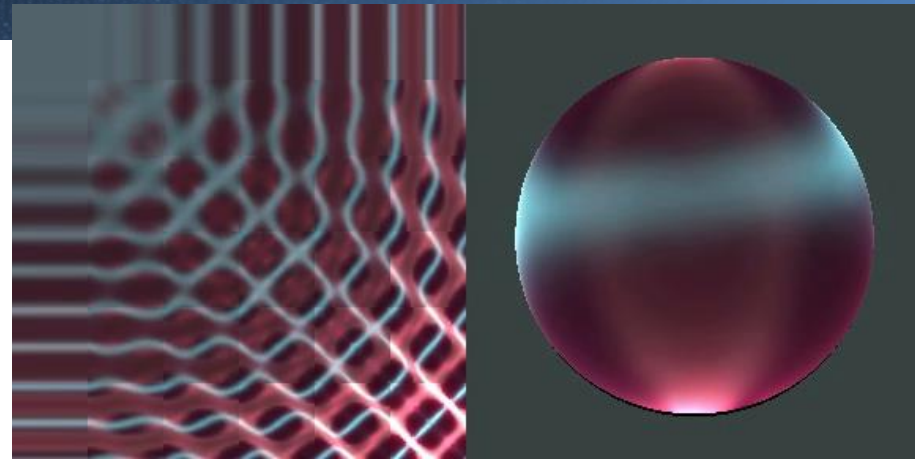
# Anisotropic Material Appearance



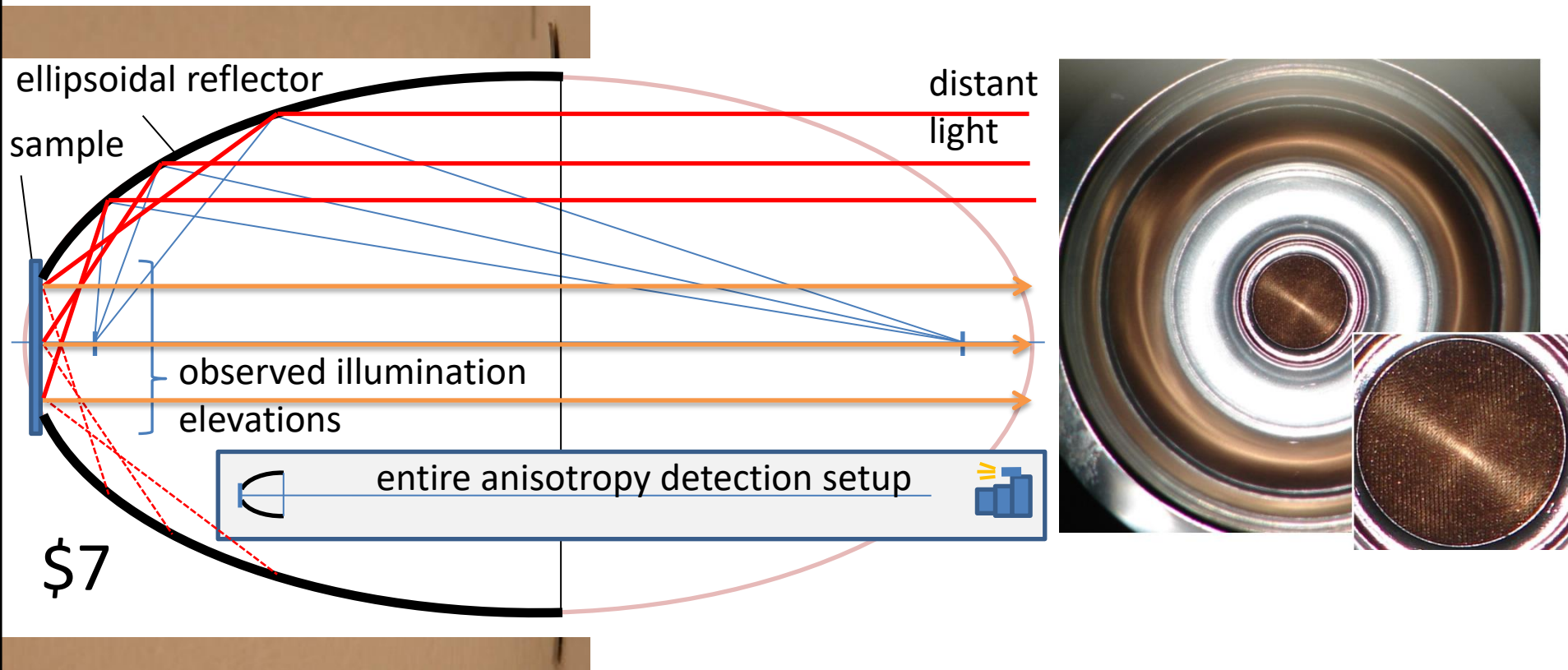
Capturing of anisotropy increases complexity of the appearance acquisition process

# Anisotropic Material Appearance

- Highlights dependent on initial position of material within appearance acquisition



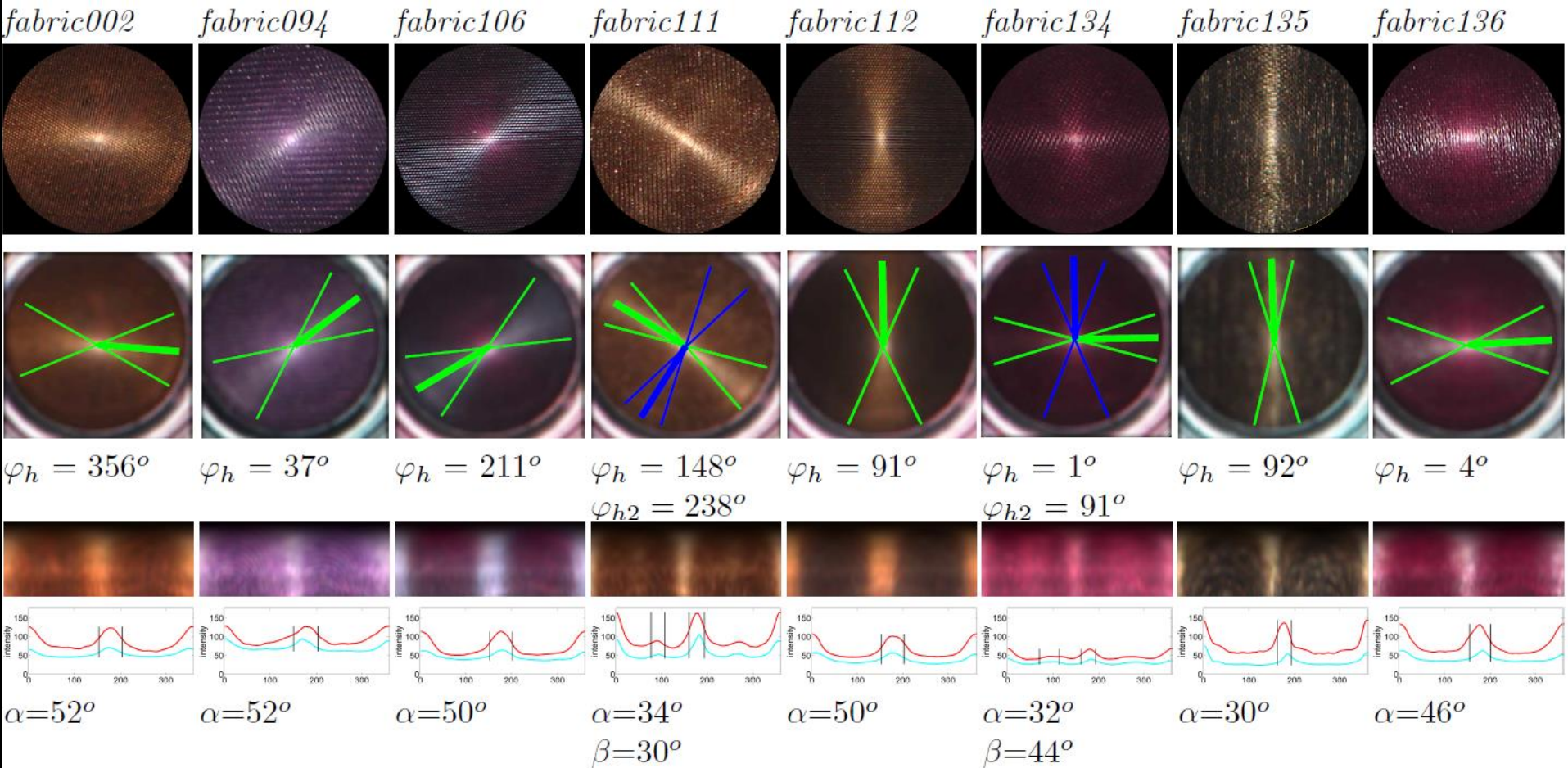
# Fast Anisotropy Detection



## Properties

- Simple setup of reflector and camera 1.5 m apart, no calibration
- Aggregated illumination using flashlight
- All illumination azimuths recorded

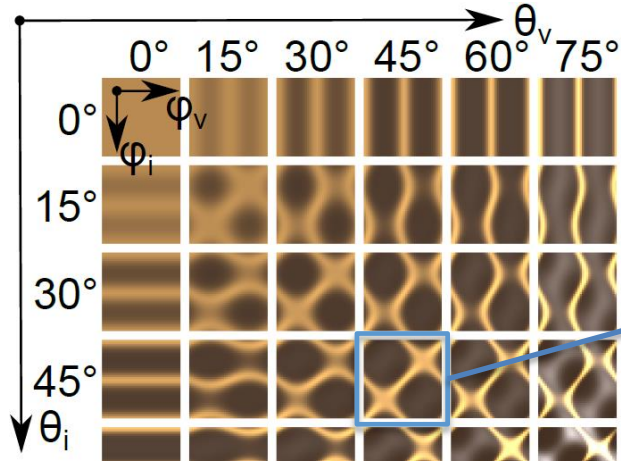
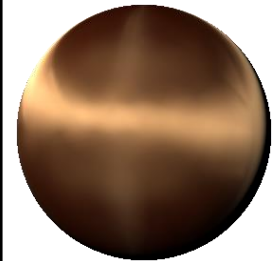
# Fast Anisotropy Detection



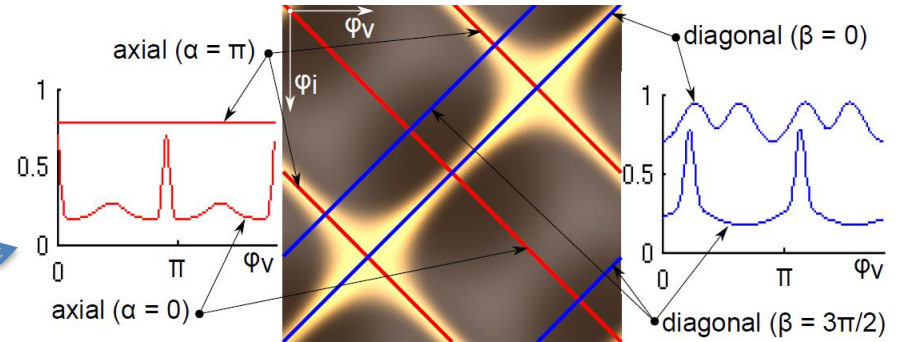
— estimated reflectance  
— reference BRDF

# Uniform vs. adaptive sampling approaches

- BRDF slices

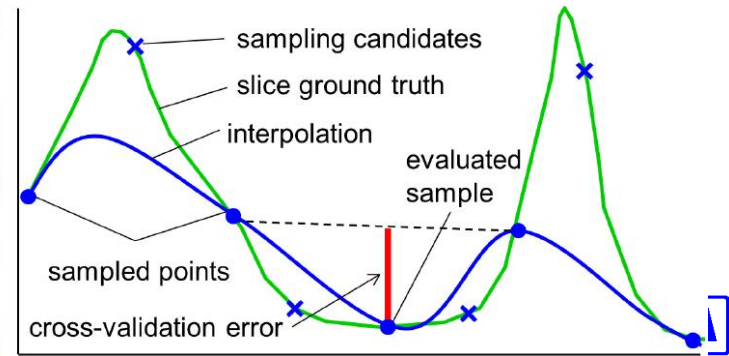
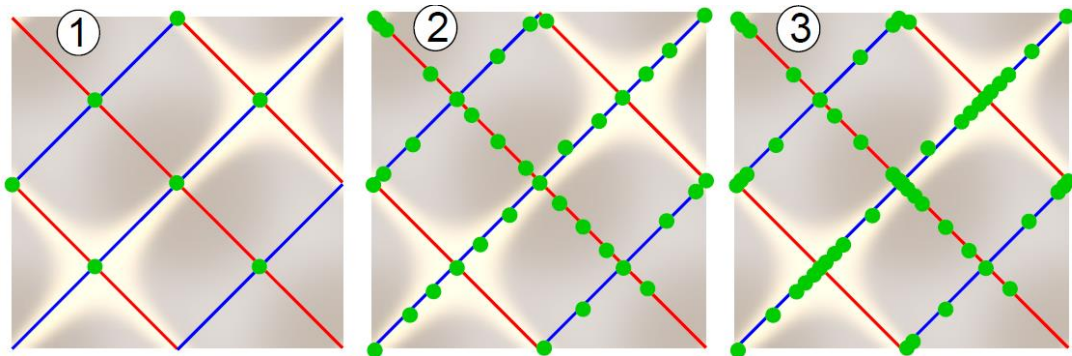


## Axial and diagonal slices (azimuths) [CVPR 13]



- Problem decomposition:** adaptive measurement of 4D function  $\Leftrightarrow$  adaptive measurement of 1D functions in 4D space

adaptive sampling based on a cross-validation error in control samples



# BRDF Data Compression

- **Splines** [He et al., SIG 92]
  - Used for storing precomputed BRDF model values
  - Do not exploit BRDF symmetry, low compression
- **Spherical harmonics** [Westin et al., SIG 92]
  - Analogy of sin,cos basis functions on sphere in frequency domain
  - Requires many parameters otherwise produces artifacts
- **Spherical wavelets** [Schroder & Sweldens, SIG 95]
  - Basis functions localized in both spatial and frequency domain
- **Zernike polynomials** [Koenderink et al., ECCV 96]
  - Polynomial functions used in optics as a basis functions mapped on hemisphere

# BRDF Data Factorization

[Kautz et al. 99] – use **SVD** to produce two 2D factors instead of 4D BRDF.

$$BRDF(\omega_i, \omega_v) \approx \sum_{k=1}^{K_j} P_{k,r_1,r_2}(\pi_1(\omega_i, \omega_v)) Q_{k,r_1,r_2}(\pi_2(\omega_i, \omega_v))$$

[McCool et al. 01] – use **Homomorphic factorization** to generate more than two positive factors.

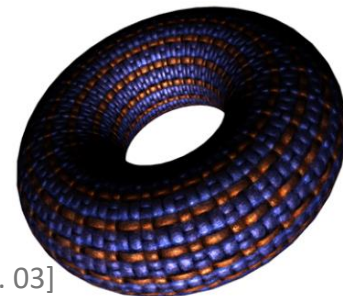
$$BRDF(\omega_i, \omega_v) \approx \prod_{j=1}^J P_{j,r_1,r_2}(\pi_j(\omega_i, \omega_v))$$

[Suykens et al. 03] – each pixel = product of three or more two-dimensional positive factors using **chained matrix factorisation**.

$$BRDF(\omega_i, \omega_v) \approx \prod_{j=1}^J \sum_{k=1}^{K_j} P_{j,k,r_1,r_2}(\pi_{j,1}(\omega_i, \omega_v)) Q_{j,k,r_1,r_2}(\pi_{j,2}(\omega_i, \omega_v))$$

✓ factors in form of textures  $\Leftrightarrow$  interactive rendering

✗ For compression of measured BRDFs only



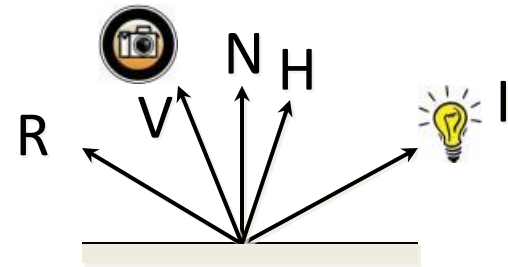
# Empirically Derived BRDF Models

- Phong shading [Phong ACM 75]
  - Ambient, diffuse, and specular terms

$$BRDF(I, V) = k_a i_a + k_d (I \cdot N) i_d + k_s (R \cdot V)^\alpha i_s$$

$k$  ... material coefs.,  $i$  ... light coefs.  $R = 2(I \cdot N)N - I$

- More computationally efficient modification [Blinn SIG 77] replaced term  $R \cdot V$  by  $N \cdot H$ . Used in OpenGL and Direct3D implementations.
- Improving energy conservation for metallic surfaces using facet-based model [Neumann et al. CGF 99].

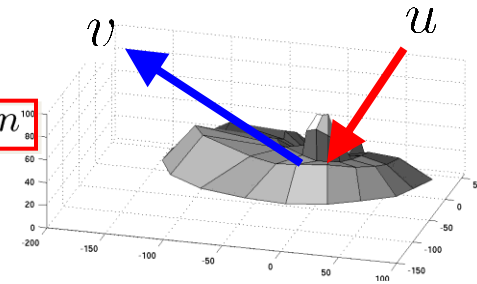




# Empirically Derived BRDF Models

- [\[Schlick EG 94\]](#) - anisotropic, energy conserving, simplified Fresnel refraction
- [\[Lafortune et al. EG 97\]](#) generalized phys. plausible cosine lobes, one lobe model as 5 params.

$$Y_{i,v} = \rho[\omega_i^T \mathbf{D}\omega_v]^n = \rho[D_x u_x v_x + D_y u_y v_y + D_z u_z v_z]^n$$



- Extension of Phong model

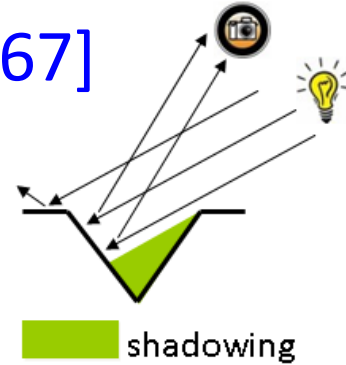
[\[Ashikhmin & Shirley JGT 00\]](#)

- non-Lambertian diffuse term, anisotropic, energy conserving, Fresnel refraction
- intuitive parameters, complex computation

# Physically-Derived BRDF Models

- **Micro-facet models** [Torrance & Sparrow JOSA 67]

- Diffuse (Lambertian lobe) and scattering parts
- Each facet – long V-cavity  $\Leftrightarrow$  perfect reflector
- Random sizes and Gaussian distribution



- Improvement [Cook & Torrance SIG 81], reflectance as

- Fresnel function  $F$
- Facet distribution  $D$
- Shadowing/Masking term  $G$

$$BRDF(\theta_i, \theta_v) = \frac{F(\theta_h)D(\theta_h)G(\theta_i, \theta_v)}{\pi \cos \theta_i \cos \theta_v}$$

- Complete model [He et al. CG 91]

- Inter-reflections, occlusions, polarization, interference, diffraction, wave effects of light, ...

☒ Isotropic reflections only

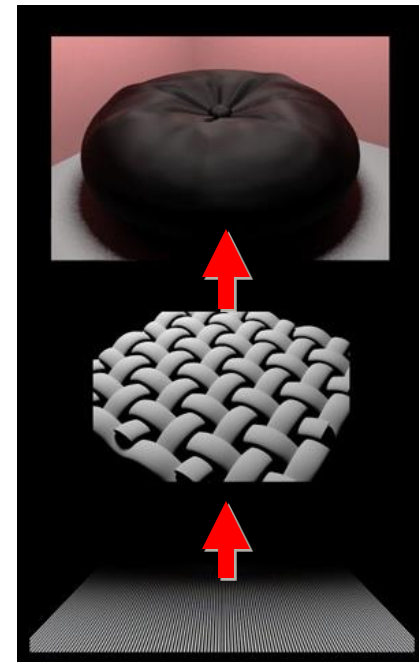
# Physically-Derived BRDF Models

- Simplified analytical microfacet model [Ward CG 92]
  - Specularity as exp() function, four physically meaningful parameters, anisotropy modeling

$$BRDF(\theta_i, \theta_v) = \frac{k_d}{\pi} + k_s \frac{1}{\cos \theta_i \cos \theta_v} \frac{e^{-\tan^2 \theta_h / \alpha^2}}{4\pi\alpha^2}$$

- normalization in [Duer 05]
- Microgeometry model [Westin 92]
  - Geometry based model  $\Leftrightarrow$  More general
  - Underlying material geometry has to be known, difficult to fit to measured BRDFs

[Westin ©ACM 92]



# Physically-Derived BRDF Models

- Model of diffuse reflection from rough surfaces  
[Oren & Nayar IJCV 95]
  - Uses [Torralca & Sparrow JOSA 67] micro-facet model,
  - Roughness as probability distribution of facet slopes,
  - Each facet has Lambertian reflectance.
- [Schlick 94 CGF 94]
  - Anisotropic, Sub-surface effects in layered materials, energy conservation
  - Account for difference between homogeneous and heterogeneous materials
  - Variable complexity formulations

# Physically-Derived BRDF Models

- [Kurt et al. CG 10] – modification of Cook-Torrance microfacet model.
  - Anisotropic extension of facet distribution, energy conservation, simple fitting, fast rendering

**Cook-Torrance:**

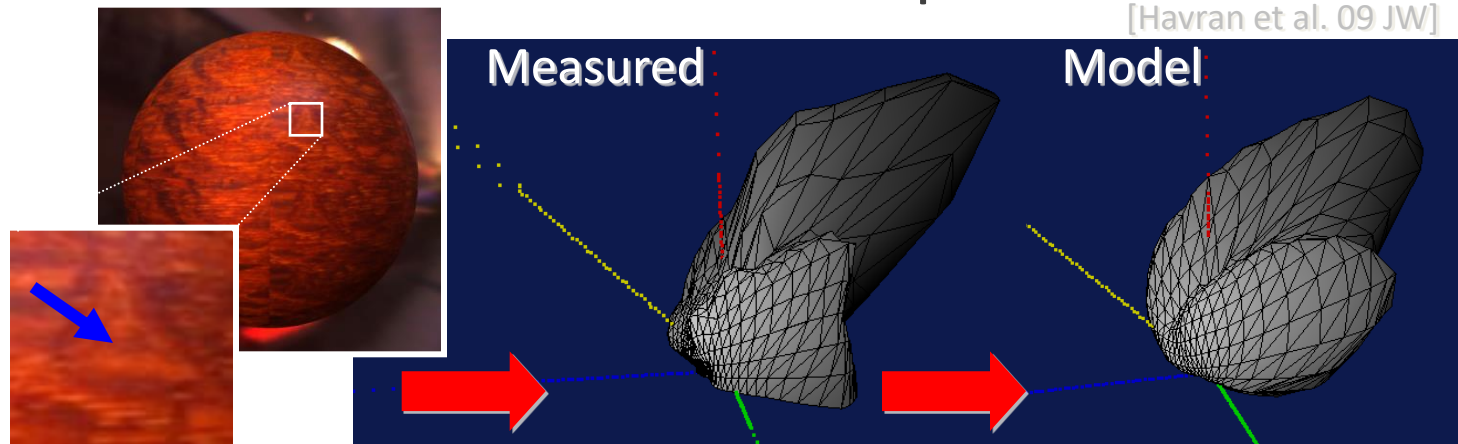
$$BRDF(\theta_i, \theta_v) = \frac{k_d}{\pi} + k_s \frac{F(\theta_h) D(\theta_h) G(\theta_i, \theta_v)}{\pi \cos \theta_i \cos \theta_v}$$

**Kurt et al.:**

$$BRDF(\theta_i, \theta_v) = \frac{k_d}{\pi} + k_s \frac{F(\mathbf{VH}) D(\theta_h, \varphi_h)}{4(\mathbf{VH})(\cos \theta_i \cos \theta_v)^\alpha}$$

# Conclusions on BRDF Modeling

- Wide range of BRDF modeling and compression techniques available
  - Non-linear iterative estimation of parameters, depends on initialization
  - Memory efficient representation of BRDF
- Results of BRDF models  $\Leftrightarrow$  low-pass filter.



- Higher quality  $\Leftrightarrow$  more parameters to store  
 $\Leftrightarrow$  often more complex fitting

# Appearance data publicly available

## BRDF Databases

- MERL BRDF database [Matusik et al. SIG03] – 100 isotropic BRDFs
- UTIA BRDF database [Vavra&Filip PG14] – 150 anisotropic BRDFs
- <http://btf.utia.cas.cz>

## BTF Databases

- CURET-Columbia&Utrecht University [Dana et al. ACM TOG99] – 61 BTFs (limited sampling directions)  
<http://www1.cs.columbia.edu/CAVE/software/curet>
- Yale University BTF database  
<http://vision.ucsd.edu/kriegman-grp/research/vst>
- University Bonn BTF database – 100 BTFs  
<http://btf.cs.uni-bonn.de/>
- UTIA BTF database [Filip et al. VC18] – 22 BTFs  
<http://btf.utia.cas.cz>

# UTIA Anisotropic BRDF Database

<http://btf.utia.cas.cz>

**6 carpet**

**96 fabric**

- upholstery
- apparel
- cushion

**10 other materials**

plaster,  
paper,  
paint, .....

**16 leather** (genuine & imitations)

**6 plastic**

**16 wood** (genuine)



# UTIA Anisotropic BRDF Database

<http://btf.utia.cas.cz>



elevation  
step =  $15^\circ$   
azimuthal  
step =  $7.5^\circ$

# UTIA BTF database – 22 materials



## BTF database

- 6 BTFs as collection of images
- 16 BTFs in BIG data format

<http://btf.utia.cas.cz>

# Conclusions on Appearance Measurement

- Measurement **setup design** depend on the required **application**
- source of errors  $\Leftrightarrow$  images registration, angular parameterization, angular sampling
- **High accuracy**  $\Leftrightarrow$  **no moving parts** or simple mechanical elements
- Maximum **sample size**  $\Leftrightarrow$  influences distance of light & camera (directional light, orthographic projection)
- Maximum **sample height**  $\Leftrightarrow$  influences selection of measurement technique (e.g. SVBRDF vs. BTF)
- Special treatment of specular and anisotropic materials
- Data-consistency-critical applications  $\Leftrightarrow$  non-uniform or adaptive sampling strategies

# Acknowledgement

## Contact

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<http://staff.utia.cz/filip>

**BTF & BRDF Data**    <http://btf.utia.cas.cz>

## Funding

- Czech Science Foundation grants No. 17-18407S, 14-02652S, 103/11/0335
- EC FP7 Marie Curie ERG 239294 (PASIMA)

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